

Dynamics of Ferroelectric Memristor Synapses

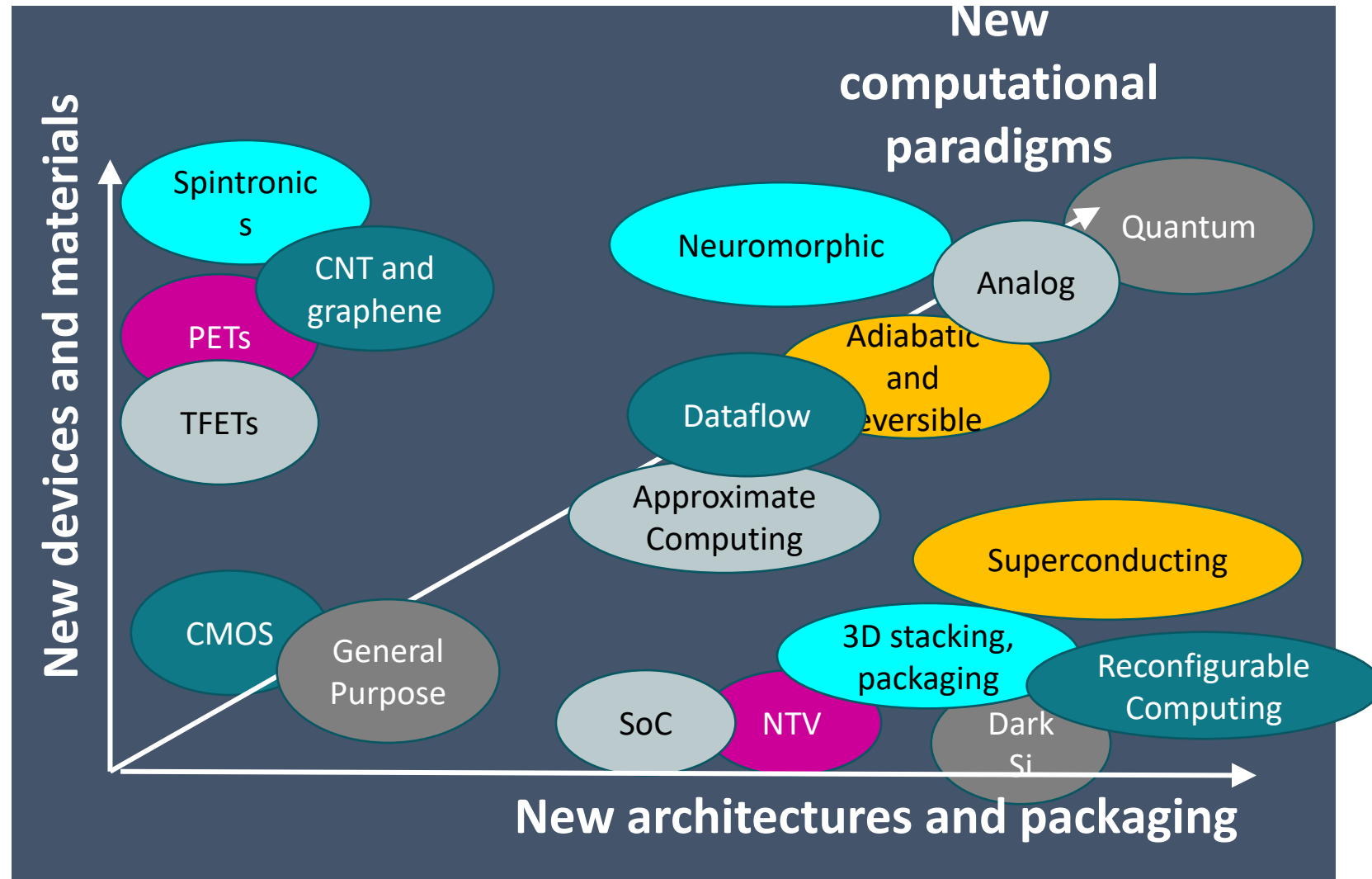
A. Dimoulas, NCSR DEMOKRITOS, Athens, Greece

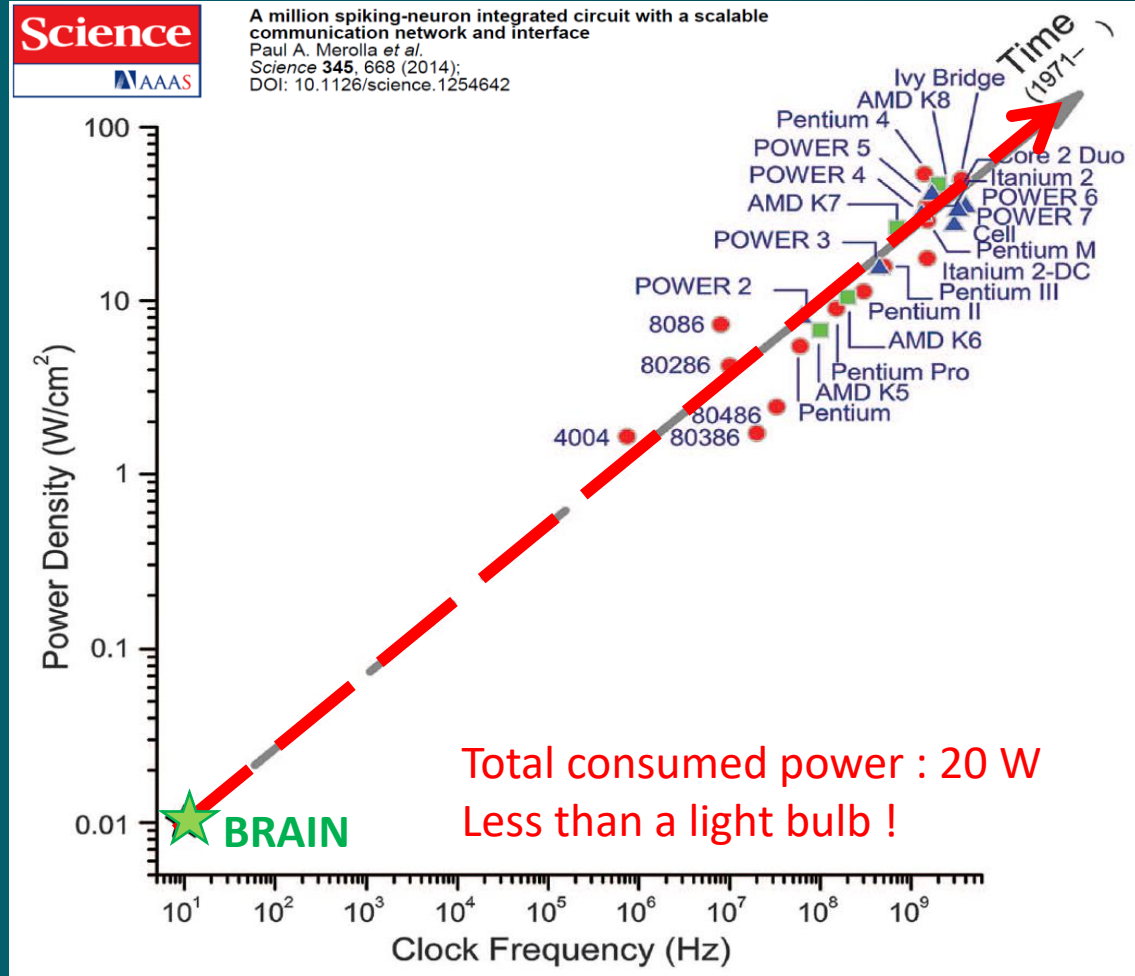


- 1 Neuromorphic Computing Technologies
- 2 Memristors-General
- 3 Ferroelectric Tunnel Junction memristors
- 4 Hafnia-based Ferroelectric Field Effect Memristor
- 5 Memristor dynamics (electronic and ionic effects)





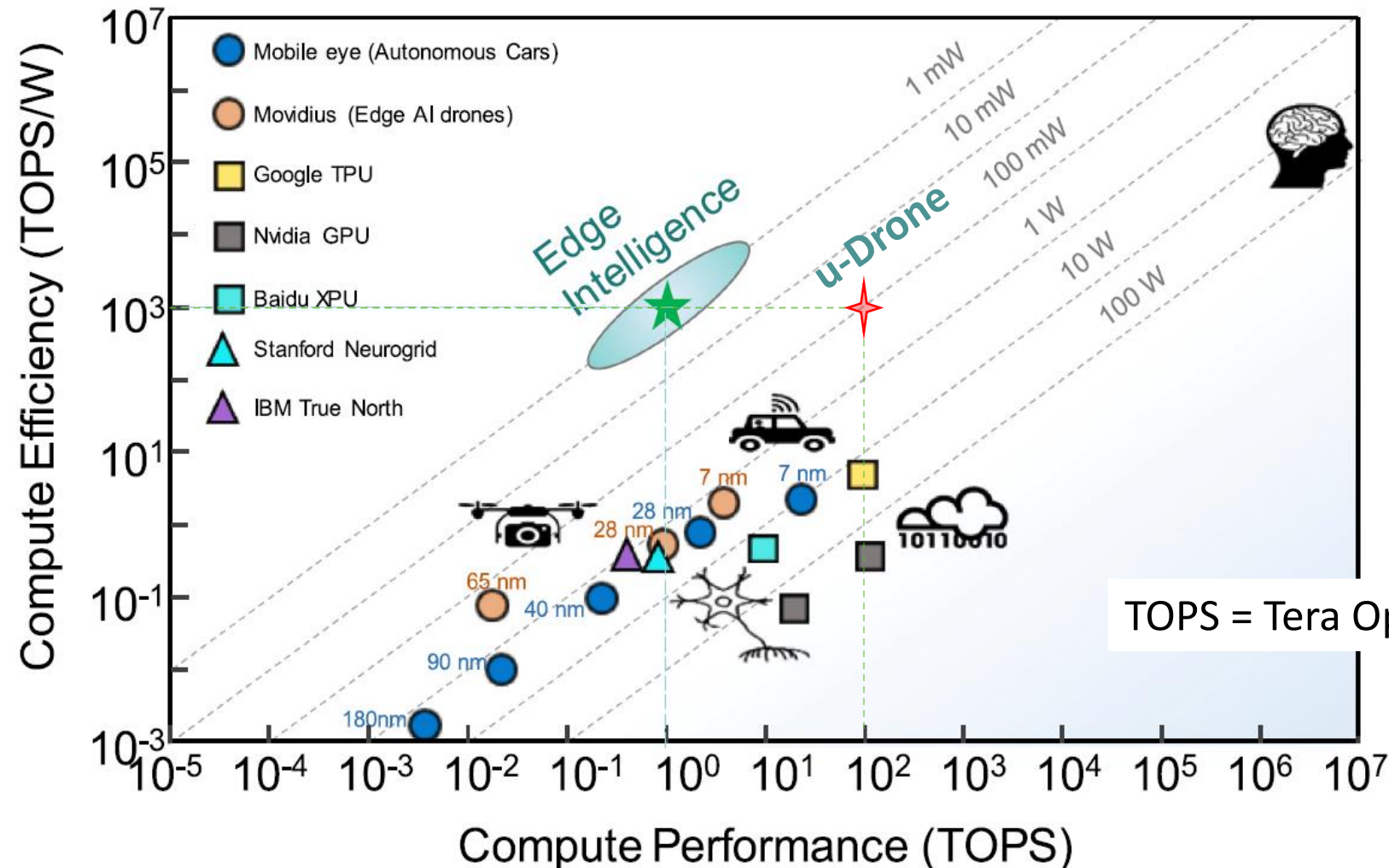




**Power
Issue**

**Von Neumann chips
are moving away
from the brain's
efficiency**

A. Keshavarzi et al., *IEEE Micro*. **40**, 1 (2020)

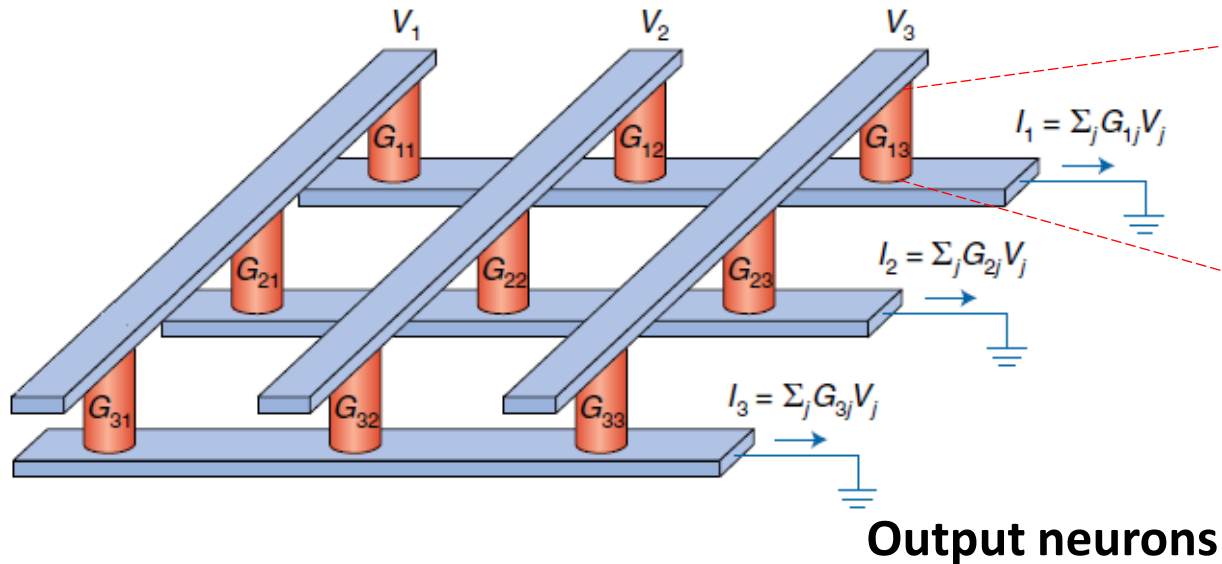


- Massive parallelism
- in-memory computing

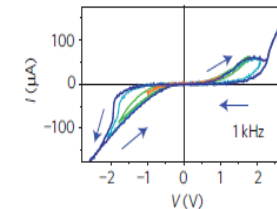
- Cross bar arrays-AI accelerators

Multiply and Accumulate

Input neurons



memristor
synapses



- Update and store conductance weights
- Analog **in-memory** computing
- Voltage driven memristors → low power

D. Ielmini, H.-S. P. Wong, *Nat. Electron.* **1**, 333 (2018)

MEMRISTOR: THE MISSING FOURTH CIRCUIT ELEMENT **FIXIT**

Resistor with memory

L.O Chua, IEEE Trans. Circuit Theory **18**, 507-519 (1971)

Generalized equations of motion

For a current controlled resistor

$$V = M(\boldsymbol{x}, I)I$$

$$\frac{d\boldsymbol{x}}{dt} = f(\boldsymbol{x}, I)$$

$\boldsymbol{x}$ = state variable

Special case

$$\boldsymbol{x} = Q \text{ (charge)}$$

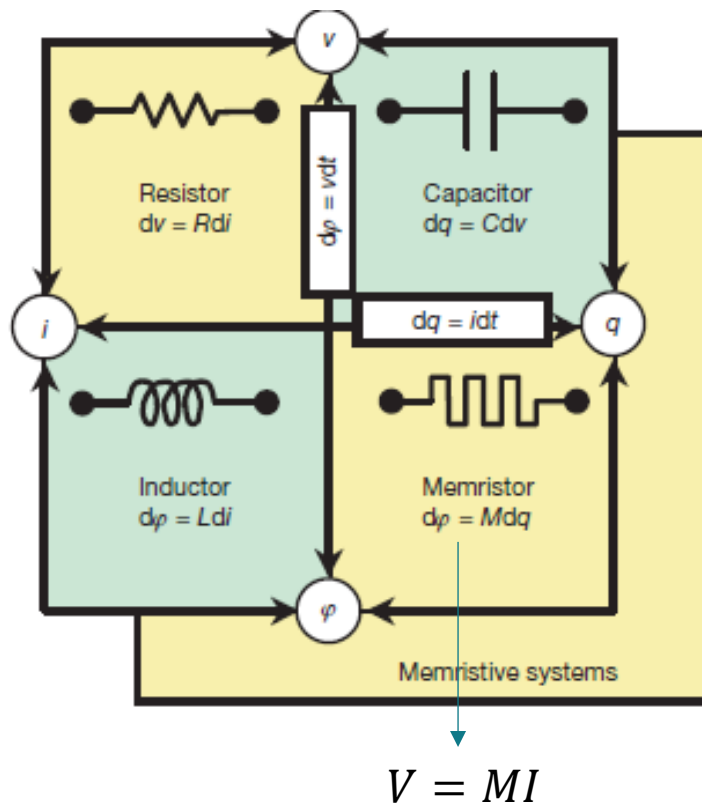
$$V = M(Q)I$$

$$\frac{dQ}{dt} = I$$

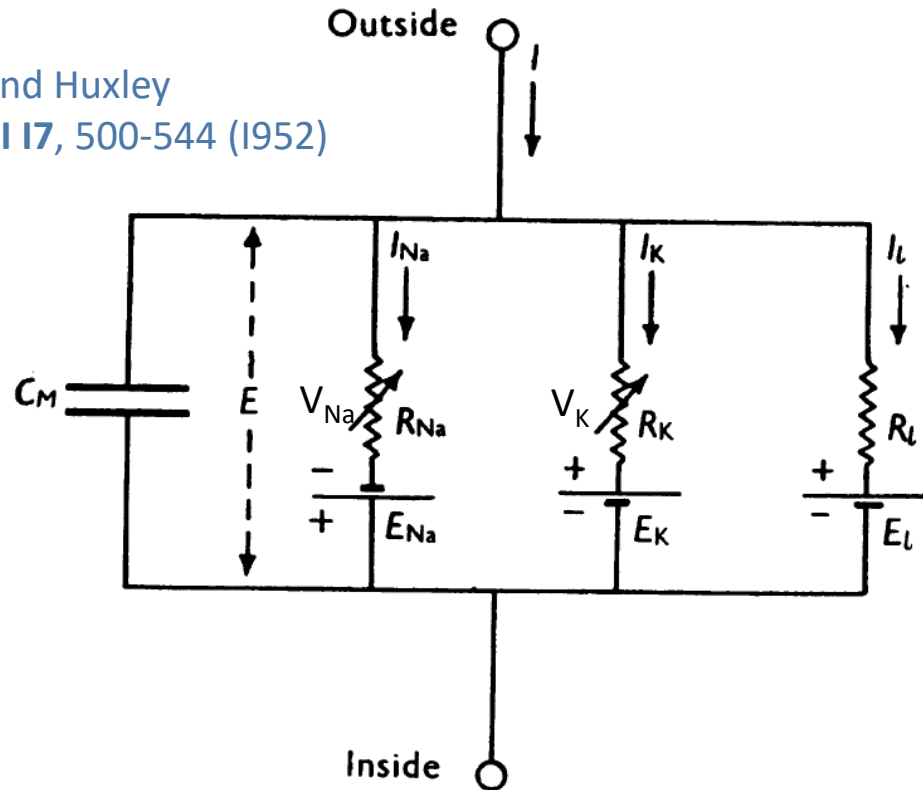
voltage controlled memristor

$$I = G(\boldsymbol{x}, V)V$$

$$\frac{d\boldsymbol{x}}{dt} = f(\boldsymbol{x}, V)$$



Hodgkin and Huxley
J. Physiol. **117**, 500-544 (1952)



$$\alpha(V_K, E_K) = -0.125 \exp\left(\frac{v_K + E_K}{80}\right)$$

$$\beta(V_K, E_K) = \frac{0.01 (v_K + E_K + 10)}{\exp[(v_K + E_K + 10)/10] - 1}$$

$$I_K = G_K(n)V_K$$

$$G_K(n) = G_{K,0}n^4$$

$$\frac{dn}{dt} = \alpha(V_K, E_K)n + \beta(V_K, E_K)(1 - n) = f(n, V_K)$$

n = K ion concentration

voltage controlled memristor $x \rightarrow n, V \rightarrow V_K$

$I = G(x, V)V$ A memristor can emulate
a biological synapse
 $\frac{dx}{dt} = f(x, V)$ as described by Hodgkin and Huxley

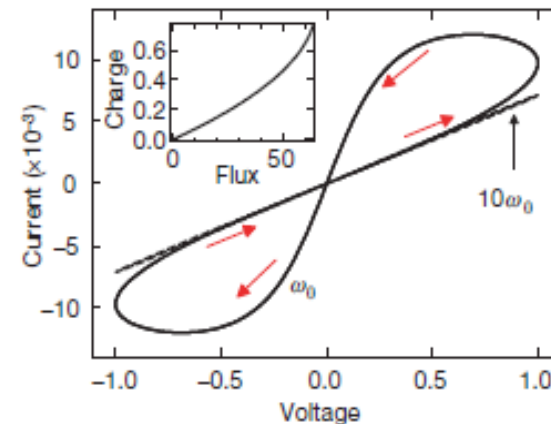
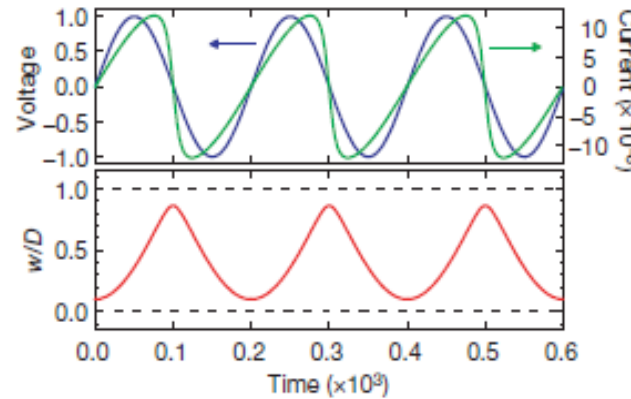
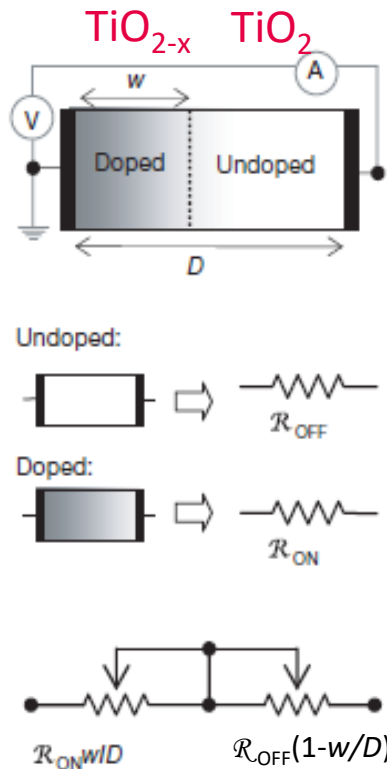
Chua and Kang Proc. IEEE 64, 209 (1976)

THE FIRST MEMRISTOR REALIZED

FIXIT

Strukov et al., *Nature* **453**, 80 (2008), Hewlett Packard

Oxygen vacancies: mobile charged dopants



$M(w(t))$ =memristance

$$V(t) = \left[R_{ON} \frac{w(t)}{D} + R_{OFF} \left(1 - \frac{w(t)}{D} \right) \right] I(t)$$

$$\frac{dw}{dt} = \mu_V E = \mu_V \frac{V}{w} = \mu_V \frac{1}{w} R_{ON} \frac{w}{D} I = \mu_V \frac{R_{ON}}{D} I$$

$$\frac{dw}{dt} = \mu_V \frac{R_{ON}}{D} I(t) \quad w(t) = \mu_V \frac{R_{ON}}{D} Q(t)$$

$$M(Q(t)) \approx R_{OFF} \left(1 - \mu_V \frac{R_{ON}}{D^2} Q(t) \right) \quad (R_{ON} \ll R_{OFF})$$

$$V = M(Q)I \quad \frac{dQ}{dt} = I$$



Funded by
the European Union

NVM FUNCTIONING AS MEMRISTORS

FIXIT

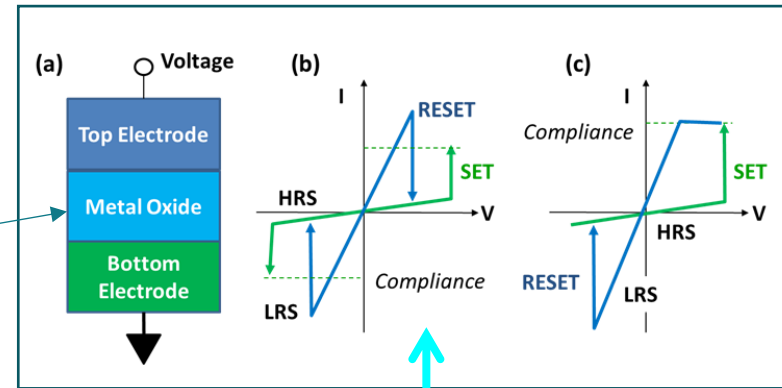
Resistive RAMs (ReRAM)

Oxide RAM (OXRAM)

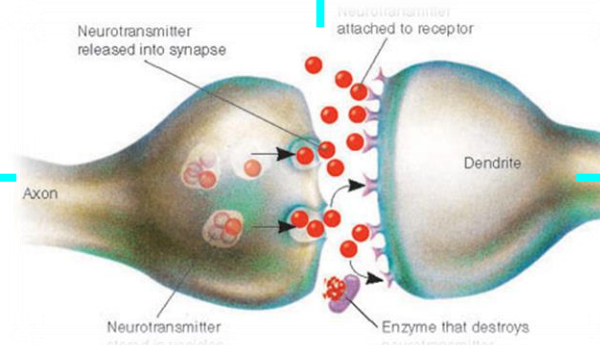
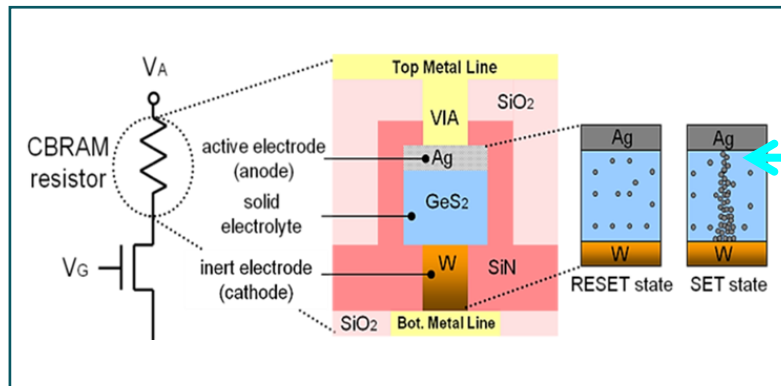
Oxygen vacancies
Electronic effect

HfO_2

Electrochemical effect
Ionic conduction

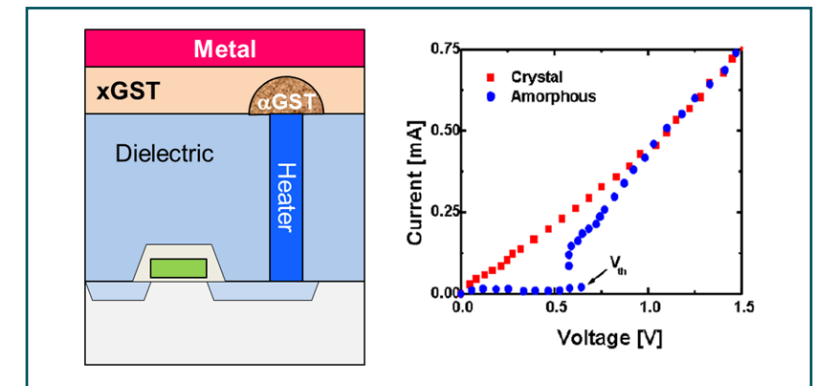


Conductive Bridge RAM (CBRAM)



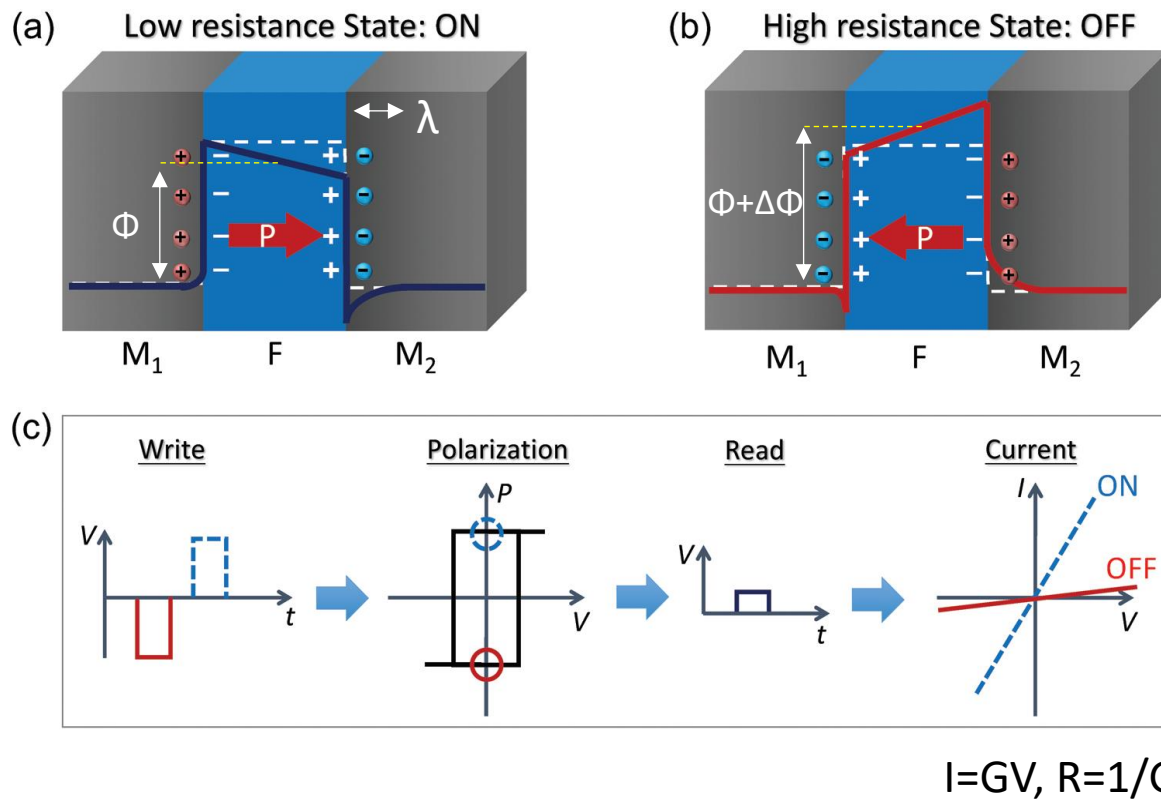
Thermal effect

Phase change RAM (PCRAM)



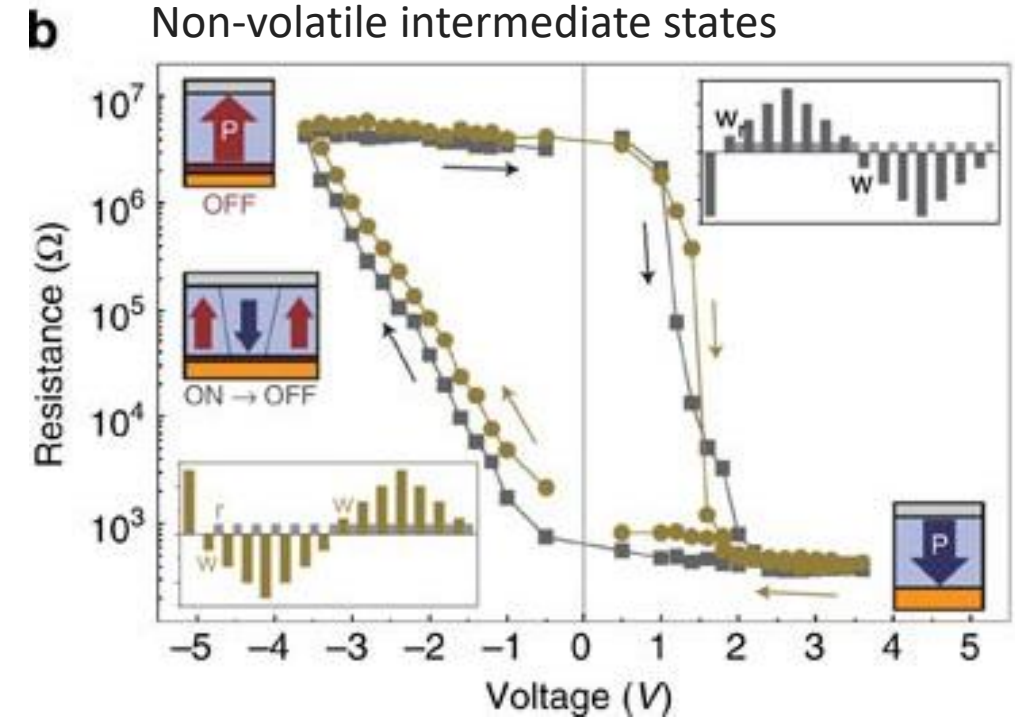
Funded by
the European Union

Z. When, D. Wu, *Adv. Mater* (2019)
<https://doi.org/10.1002/adma.201904123>



V. Garcia, M. Bibes
Nature Commun. **5**, Article No 4289 (2014)

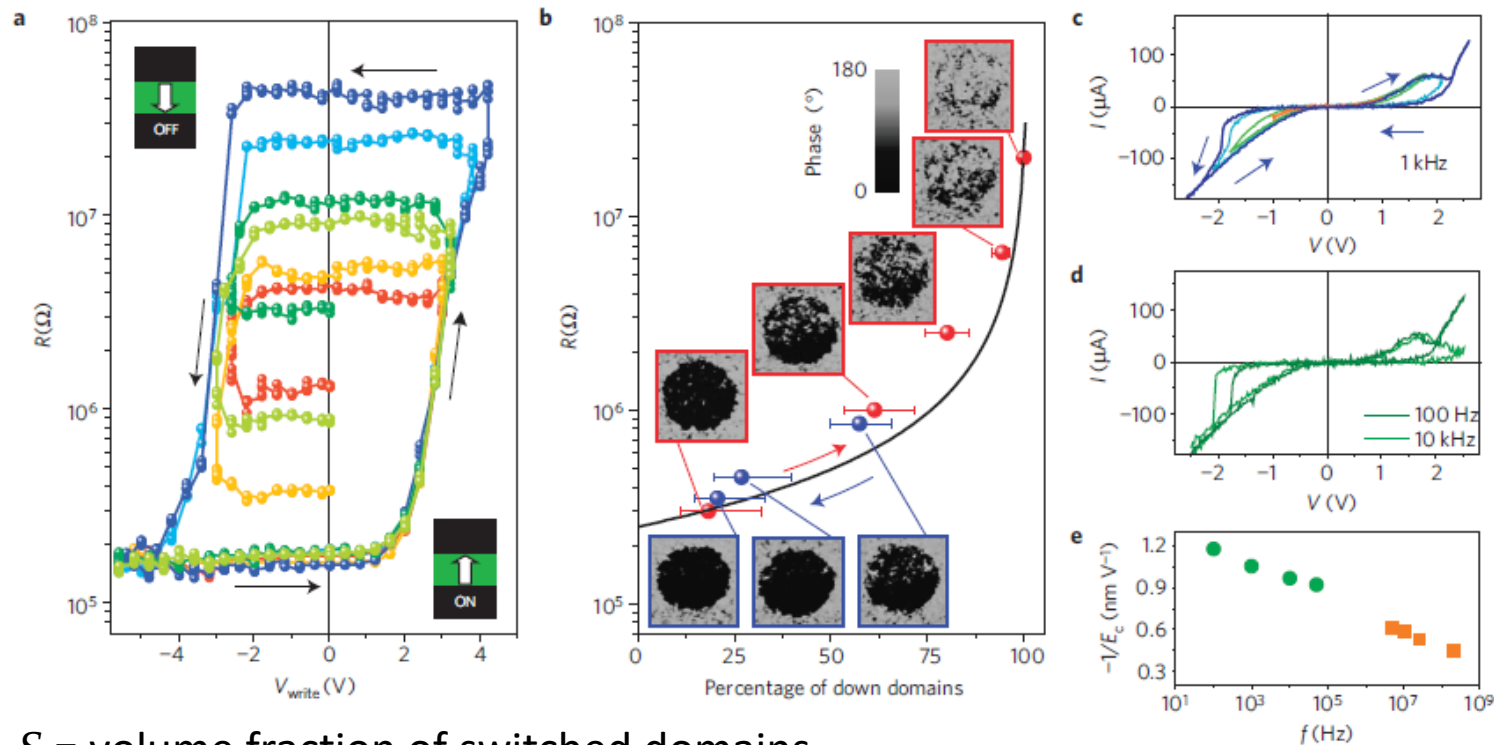
Partial polarization:
 Non-volatile intermediate states



THE FIRST FERROELECTRIC MEMRISTOR

FIXIT

A. Chanthbouala et al., *Nat. Mater.* (2012) DOI: 10.1038/NMAT3415



S = volume fraction of switched domains

$$s = \sum_{i=1}^{N(i)} S_i * h(t - \tau_N^i) * \left\{ 1 - \exp \left[- \left(\frac{t - \tau_N^i}{\tau_p^i} \right)^2 \right] \right\}$$

$$ds/dt = (1-s) \times \left\{ \frac{2}{\tau_p(V)} \left(\frac{t - \tau_N(V)}{\tau_p(V)} \right) \right\} = f(s, V, t)$$

$$V(t) = R(\sigma, V, i) i(t)$$

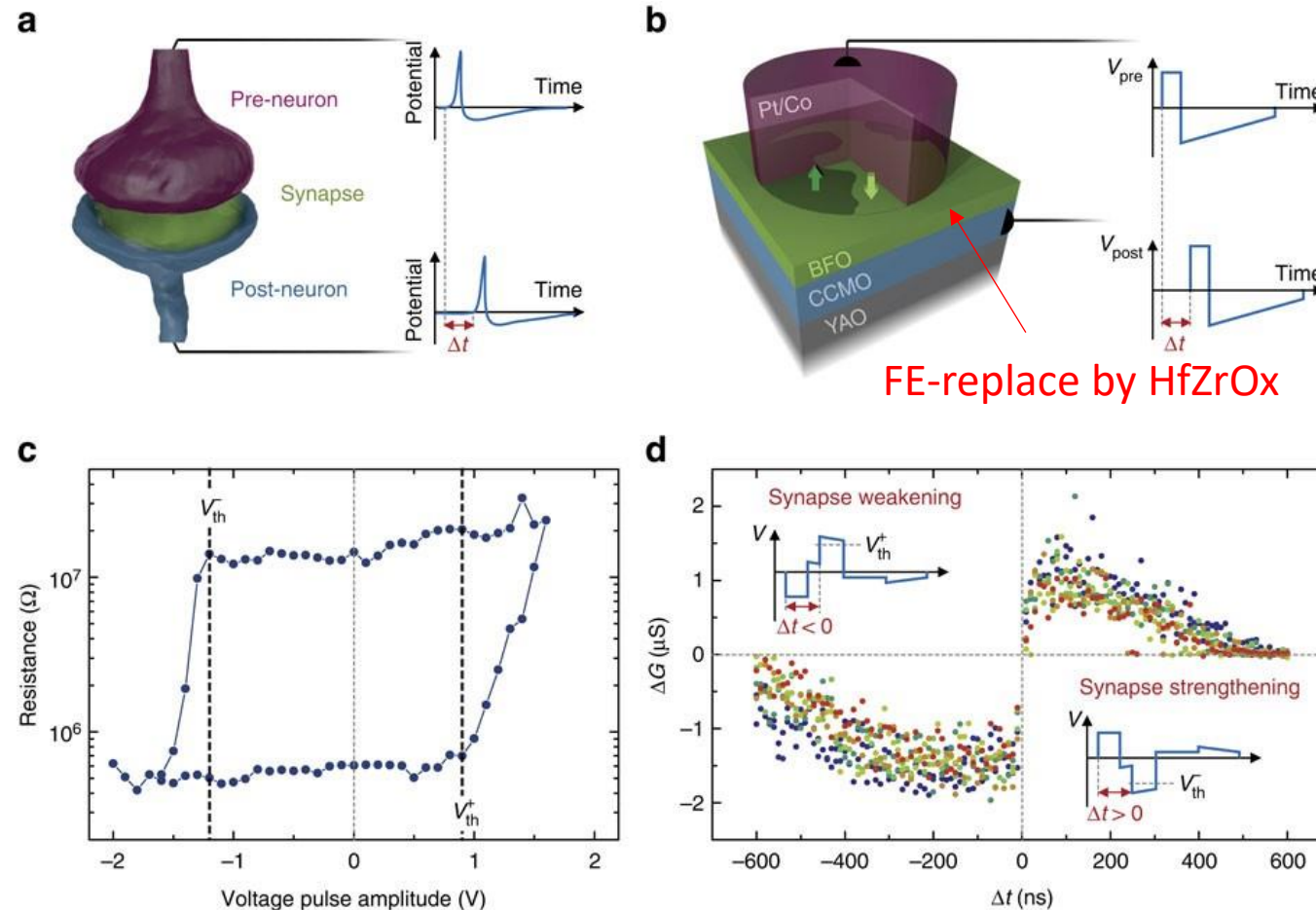
$$d\sigma/dt = f(\sigma, V, t)$$



Funded by
the European Union

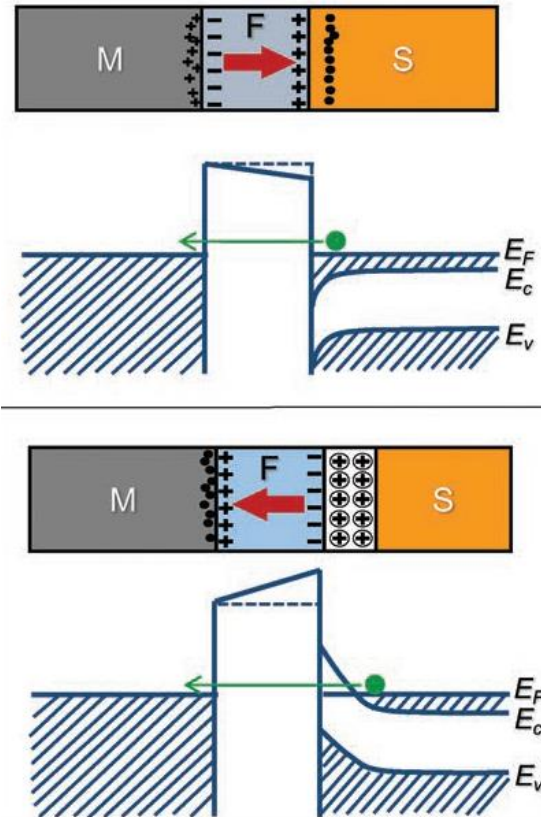
Unsupervised learning with ferroelectric synapses

S. Boyn et al., *Nature Commun* 8, Article number: 14736 (2017)

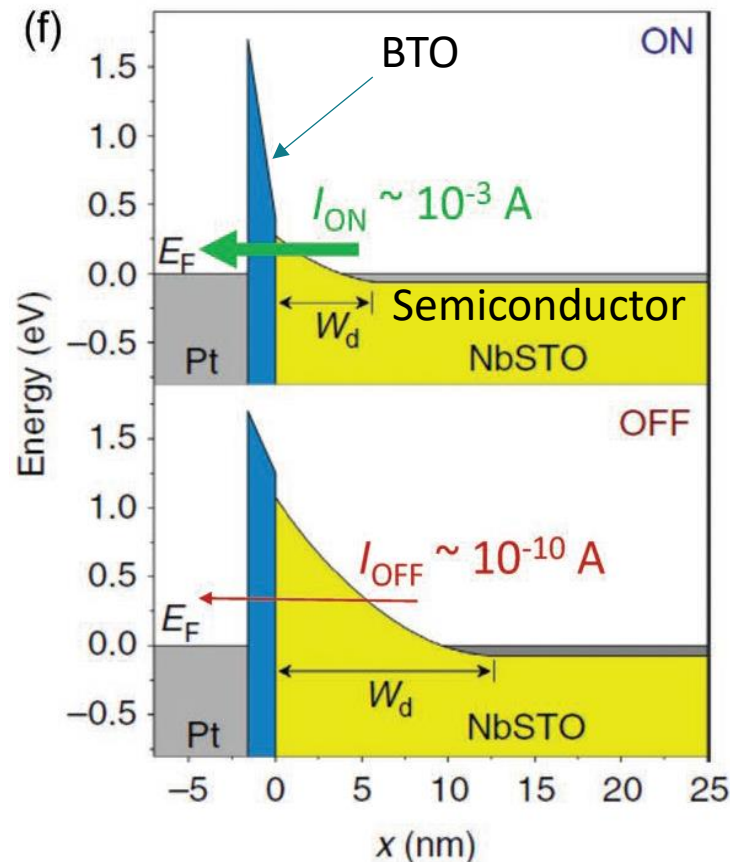


STDP activity-fast response

Z. Wen et al., *Nat. Mater.* **12**, 617 (2013)



Z. Xi, et al., *Nat. Commun.* **8**, 15217 (2017)



- MFS/FTJ: best performance - **Giant TER** $> 10^7$
- Predominant effect of Schottky barrier for thin FE

FIXIT

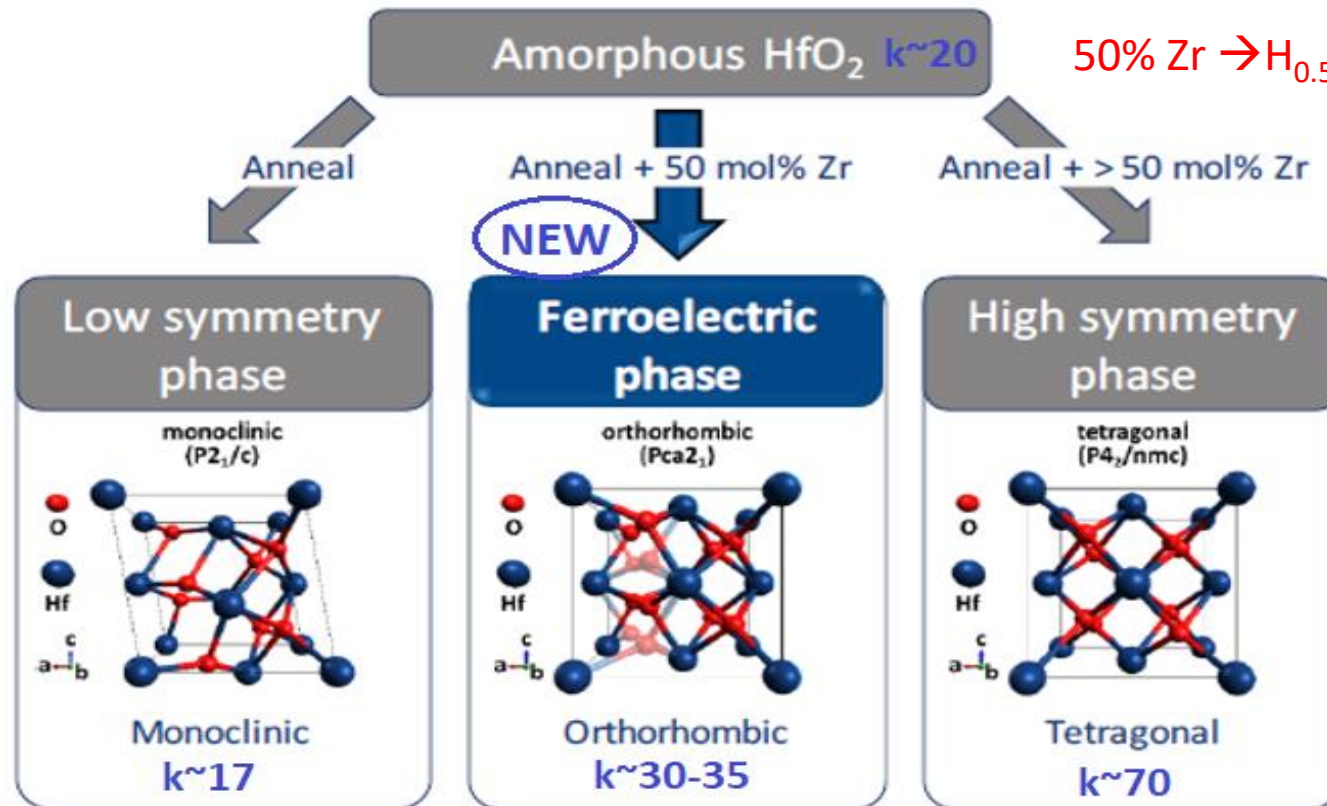
[illegible]

W/Zr:HfO₂/SiO₂/Si
S.S. Cheema et al., *Nature* (2020)

-  Ref.117
 2015
 Ref.36
 Ref.40
 Ref.46*
 Ref.62*
 0  Ref.118

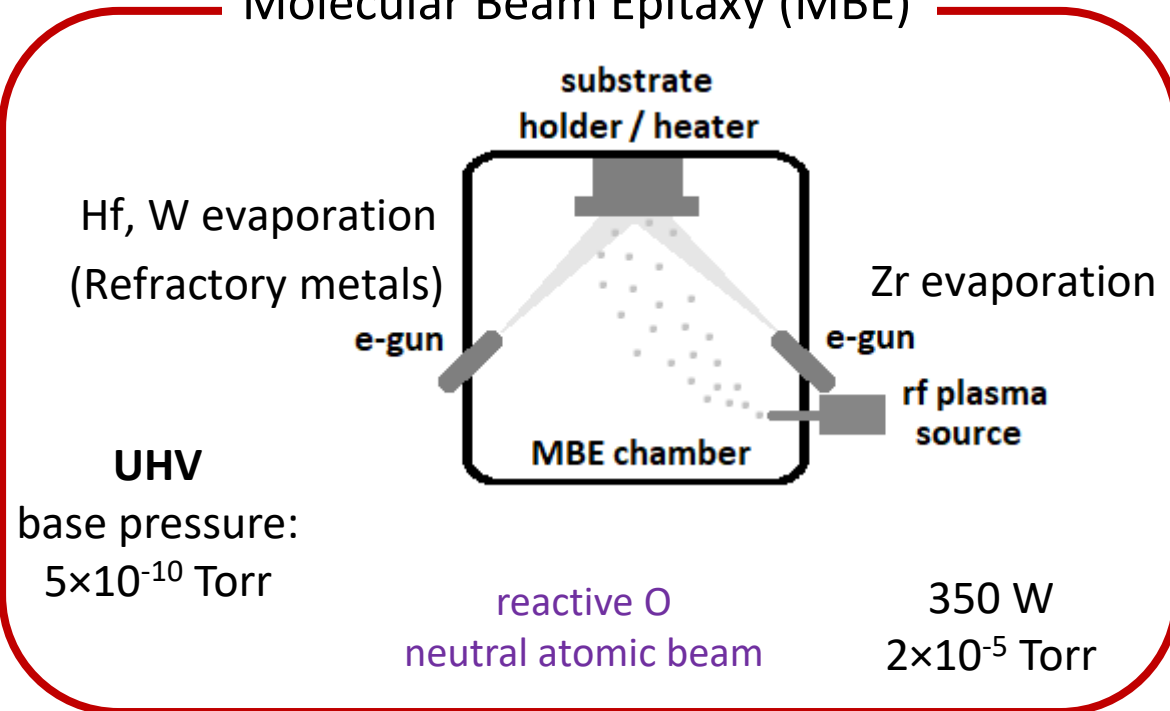
Discovered in 2007-first published 2011, Qimonda [T. S. Böске et al, Appl. Phys. Lett. 99, 102903 \(2011\)](#)

Stabilization of the ferroelectric phase: doping (Si, Zr,..), stress, annealing, film thickness ...



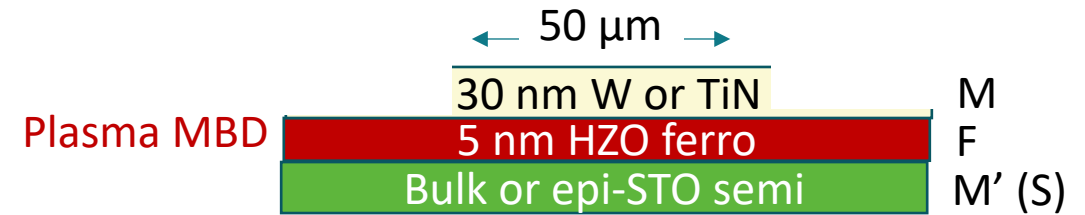
Compatible with Si processing
(HfO_2 used as high-k dielectric/CMOS scaling)

Molecular Beam Epitaxy (MBE)



C. Zacharaki et al., *Appl. Phys. Lett.*, **114**, 112901 (2019)

C. Zacharaki et al., *ACS Appl. Electron. Mater.* **4** 2815 (2022)



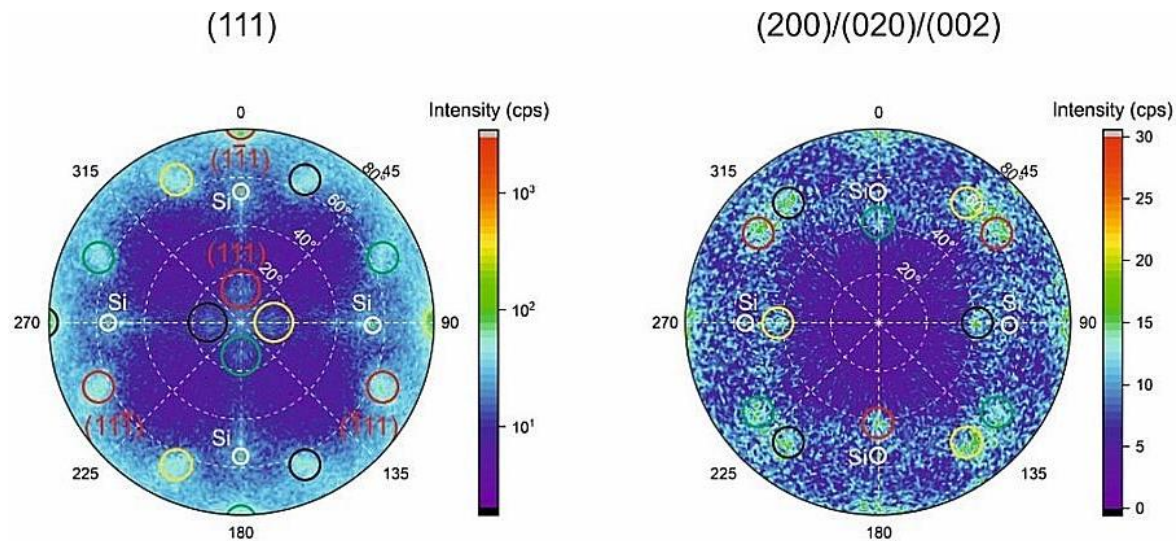
Bulk : Nb:STO

Epi-STO on Si (001)

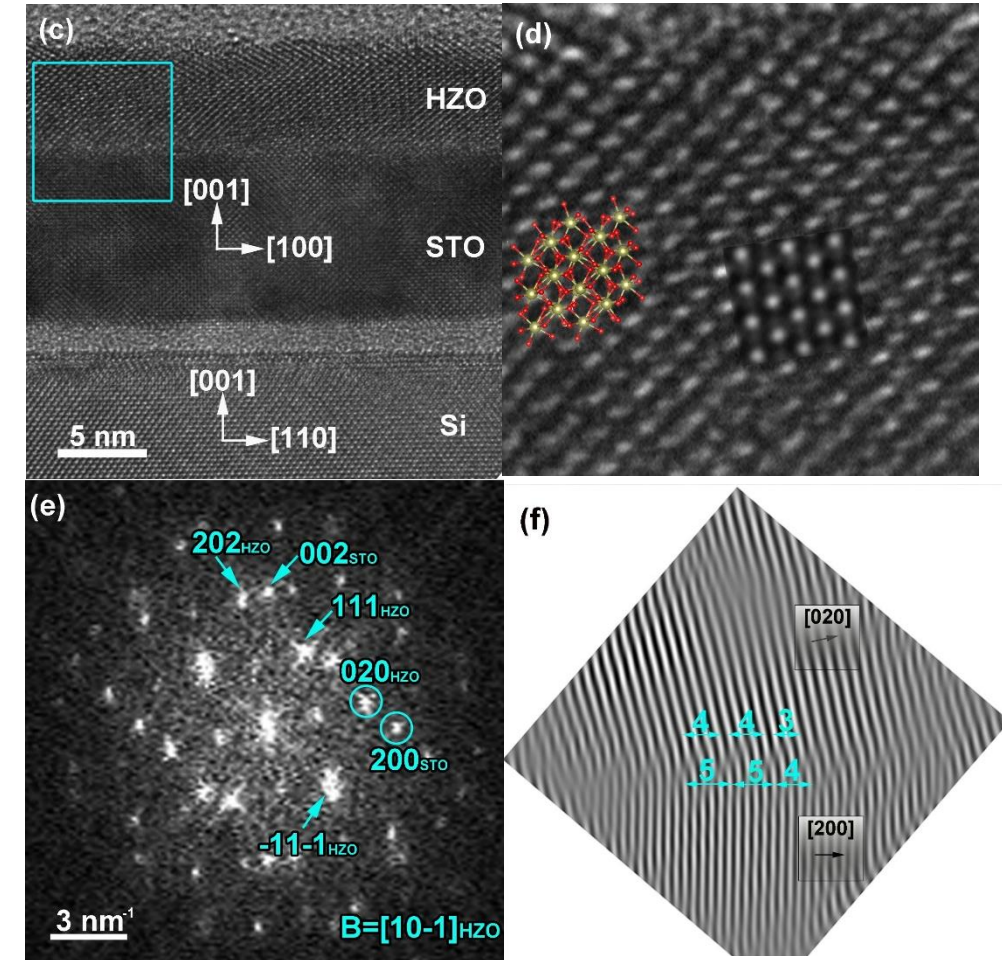
- Deliberately grown O deficient to act as bottom electrode
- O vacancy donors $V_O=0.56\%$ $\rightarrow$ N-type $\rho=0.02 \Omega\text{cm}$

- $T_{\text{growth}}(\text{HZO})=120^\circ\text{C}$, amorphous
- Crystallization annealing 420°C , 400 s $\rightarrow$ **Epitaxial**
- Optical litho + etching or lift-off

XRD pole figures



- [111] HZO 15 deg off vertical
- 0, 90, 180, 270 deg rotated domains due to 4-fold symmetry of STO substrate

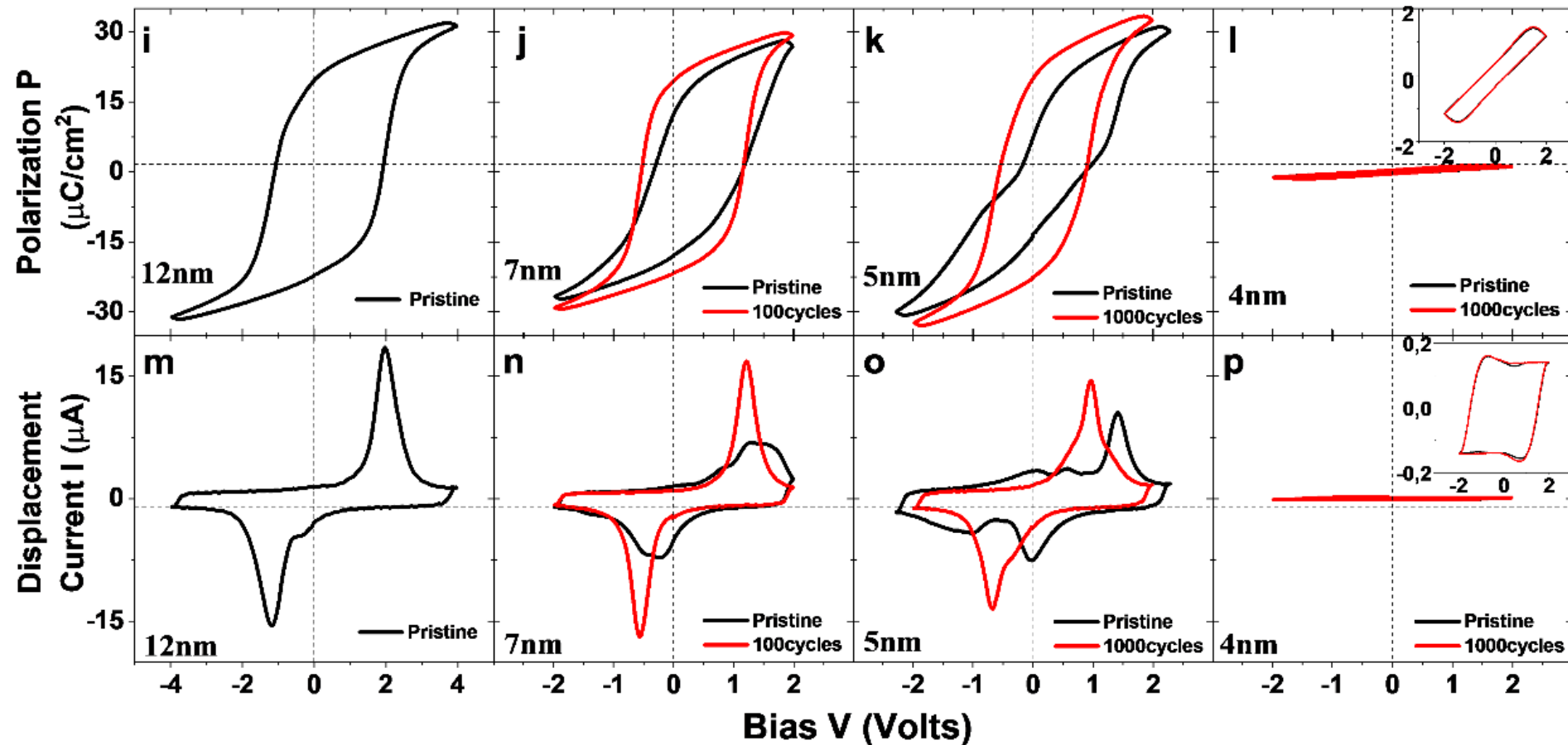


Domain Matching Epitaxy

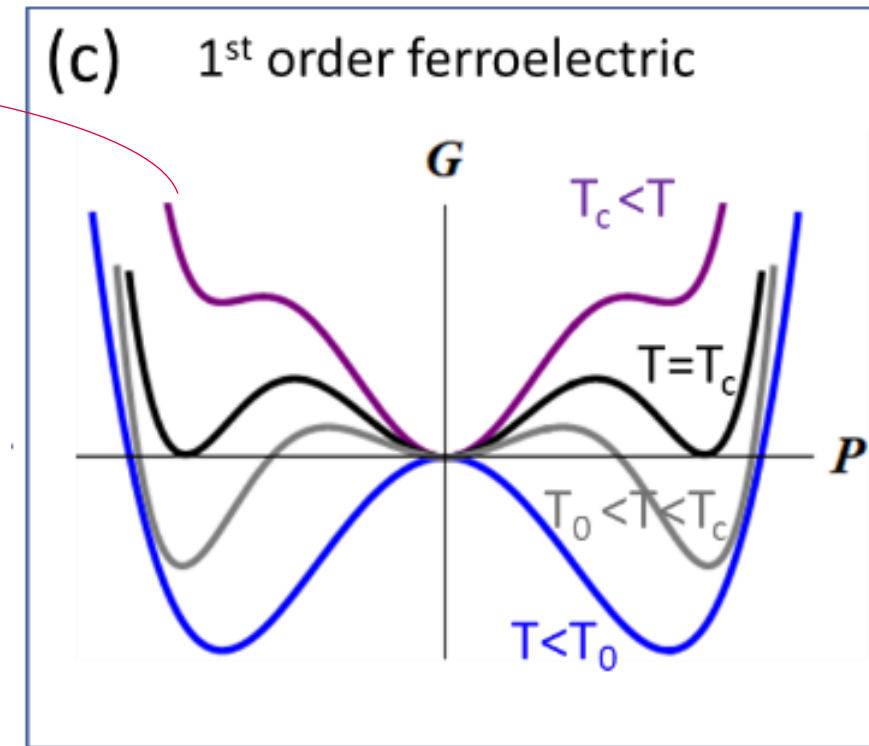
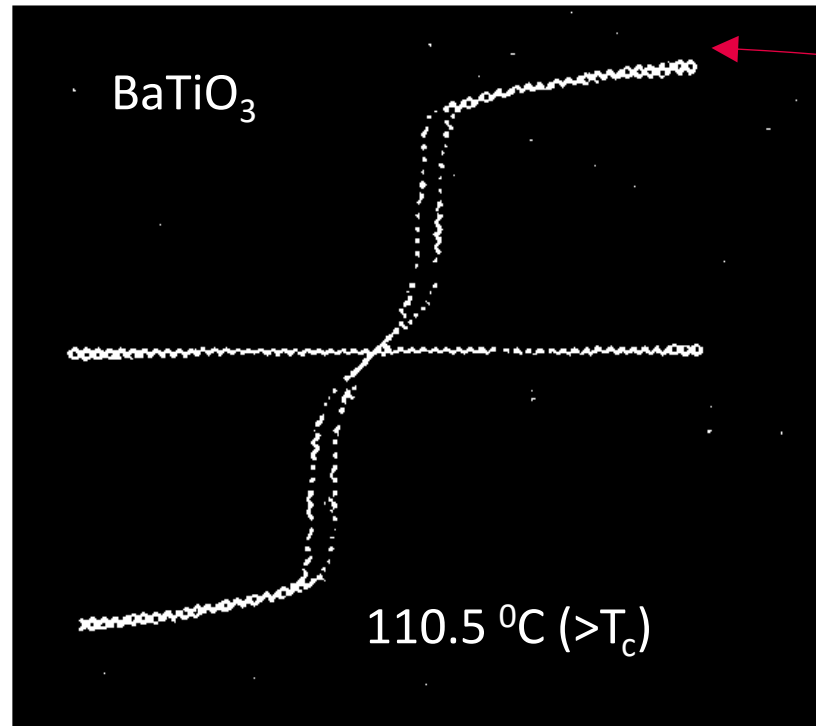
S. Estandia et al., *Cryst. Growth Des.* **20**, 3801 (2020)

Nb:STO/HZO/TiN

Below 5 nm HZO, ferroelectricity is unstable [N. Siannas et al., *Comms. Phys.* 5, 178 \(2022\)](#)



Walter J. Merz, *Phys. Rev.* **91**, 513 (1953)

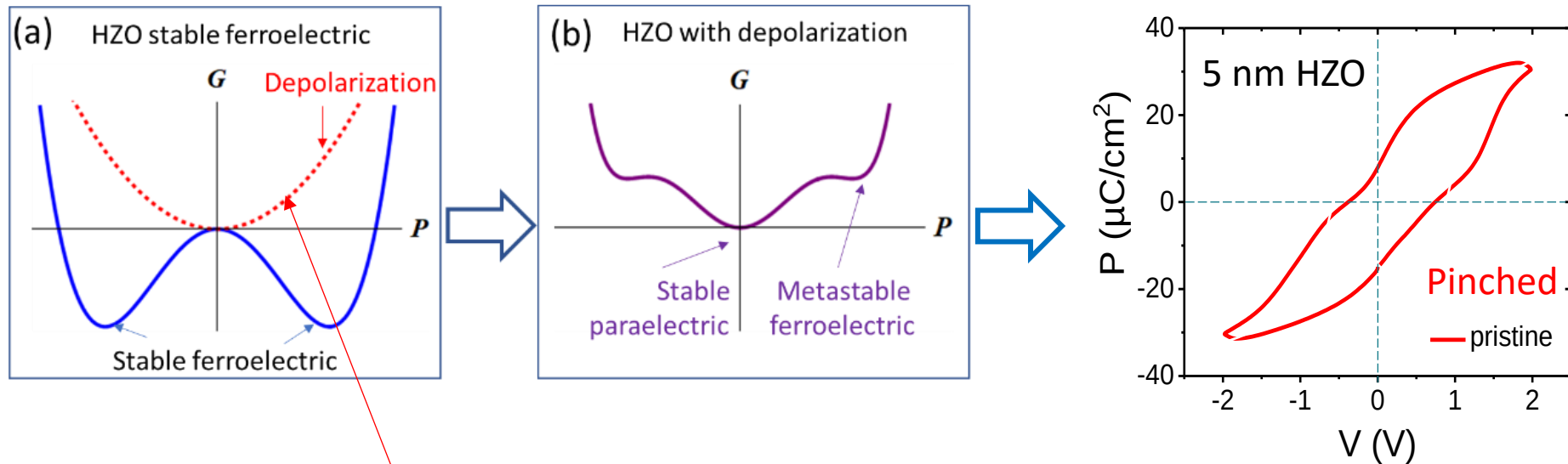


Double loop behavior originates from triple potential well slightly above T_c

DEPOLARIZON INDUCED METASTABLE FERROELECTRICITY **FIXIT**

N. Siannas et al., *Comms Phys* 5, 178 (2022)

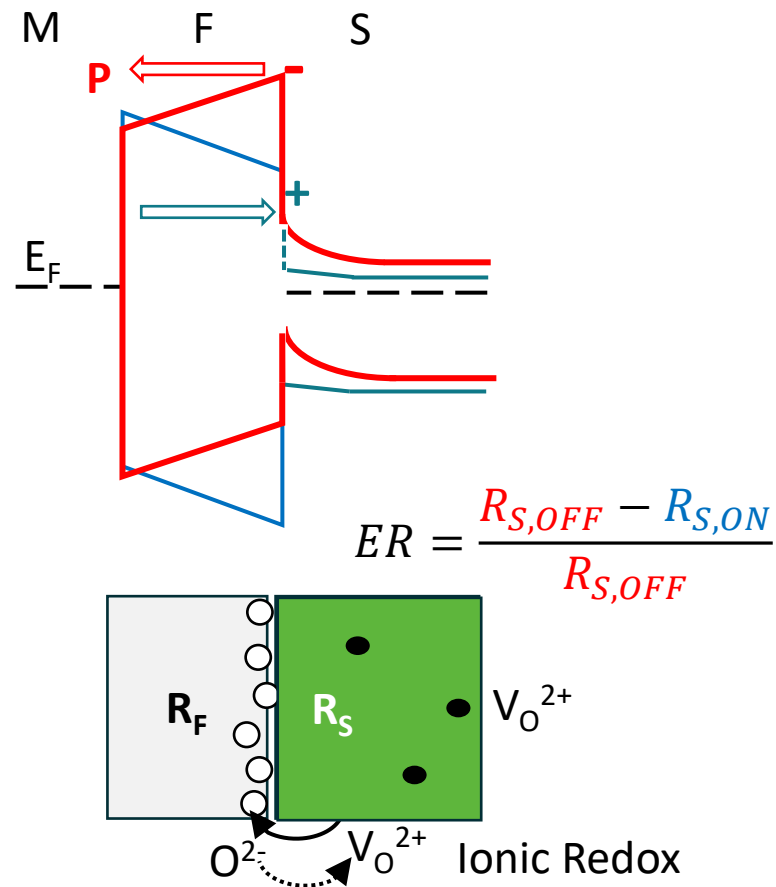
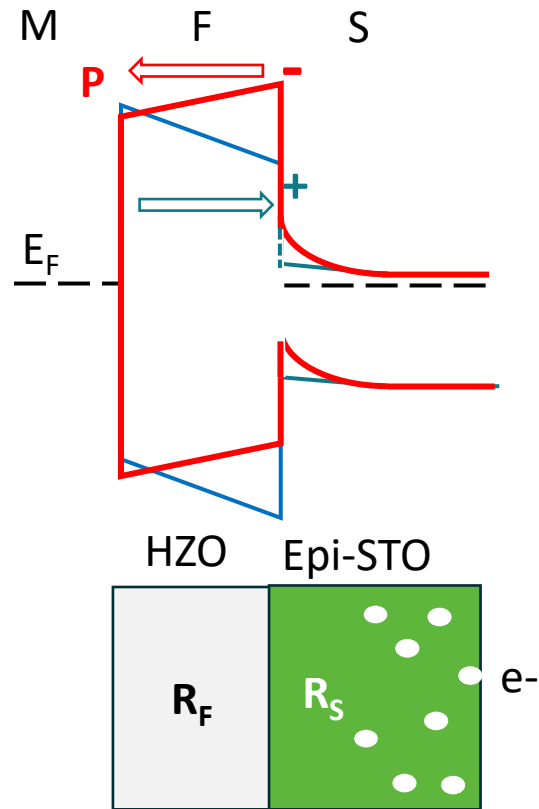
HZO with depolarization resembles a 1st order FE above T_c



$$G = -\frac{1}{2}|a|P^2 - \frac{1}{4}|\beta|P^4 + \frac{P^2}{\epsilon_0\epsilon_F\left(1 + \frac{C_{int}}{C_F}\right)} + \frac{1}{6}\gamma P^6$$

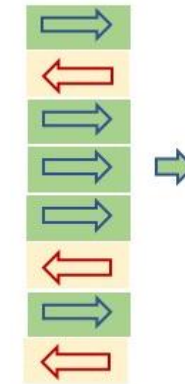
- Ferroelectric programming of the semiconductor resistance

N. Siannas et al., *Adv. Funct. Mater.* (2023); doi: 10.1002/adfm.202311767

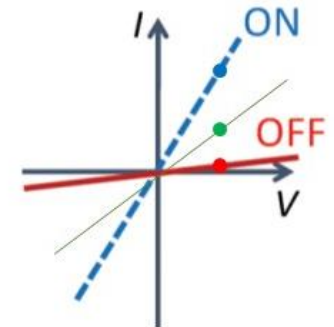


$$ER = \frac{R_{S,OFF} - R_{S,ON}}{R_{S,OFF}}$$

Partial Polarization

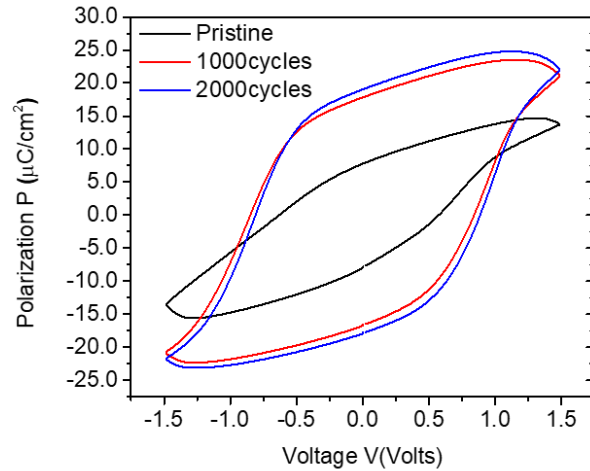


Intermediate NV resistance states

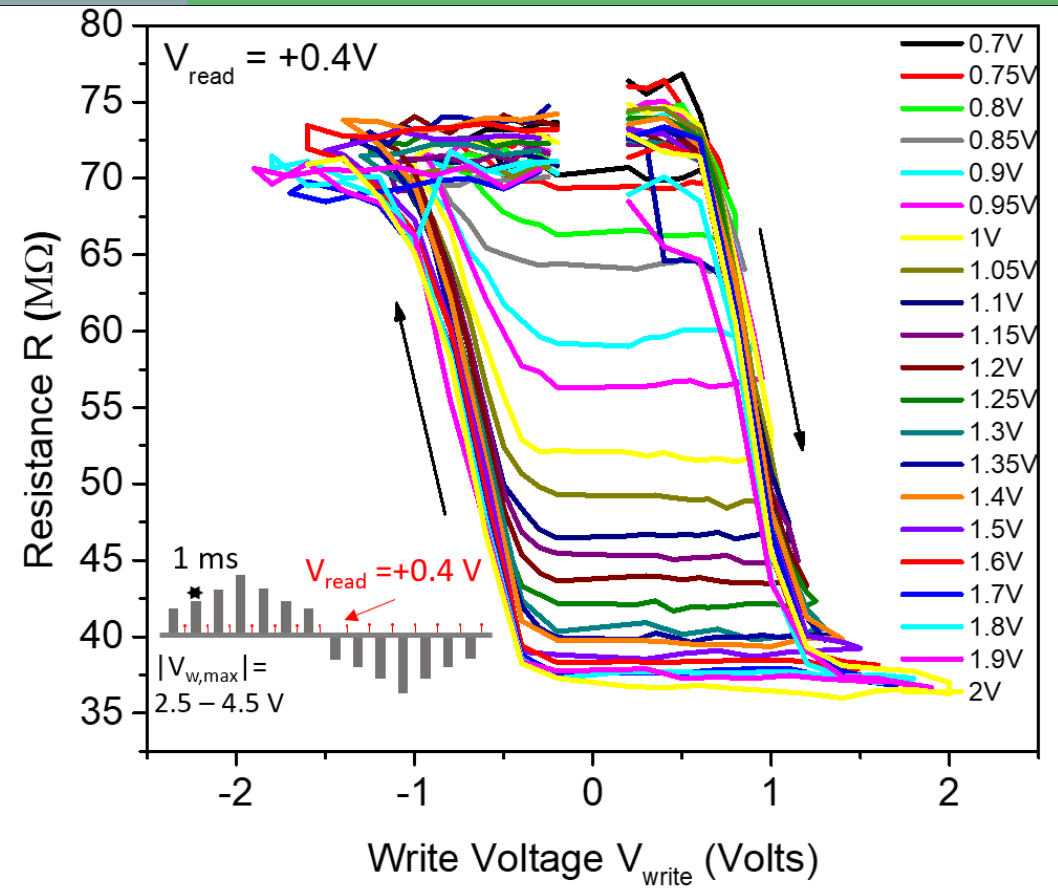
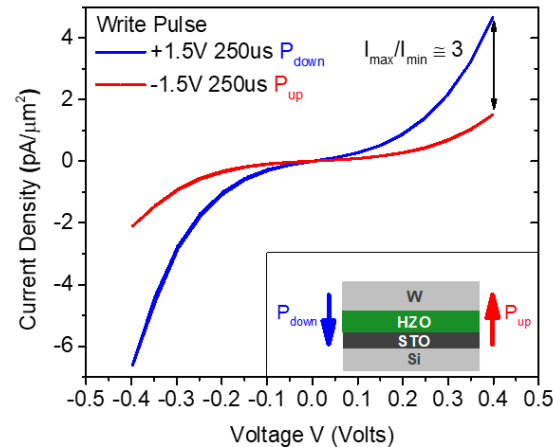
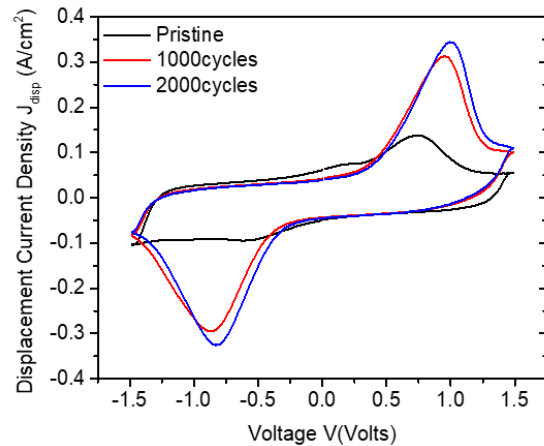


MAIN CHARACTERISTICS

FIXIT



- $P_r \sim 14 \mu\text{C}/\text{cm}^2$
- $V_c < 1\text{V}$
low voltage operation
- Low $I_{\text{ON}} / \text{low ER}$

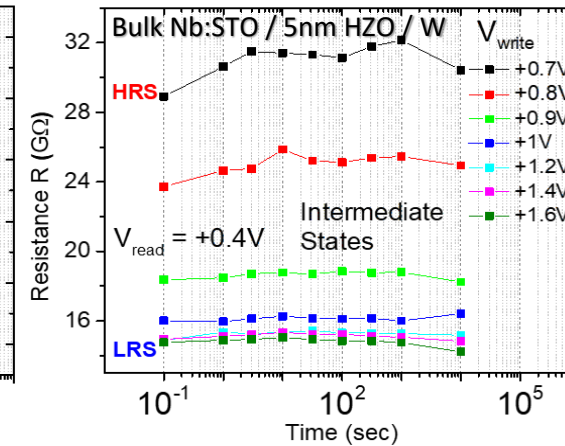
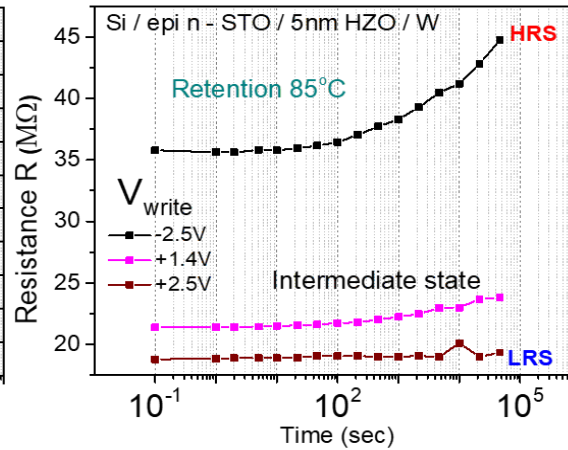
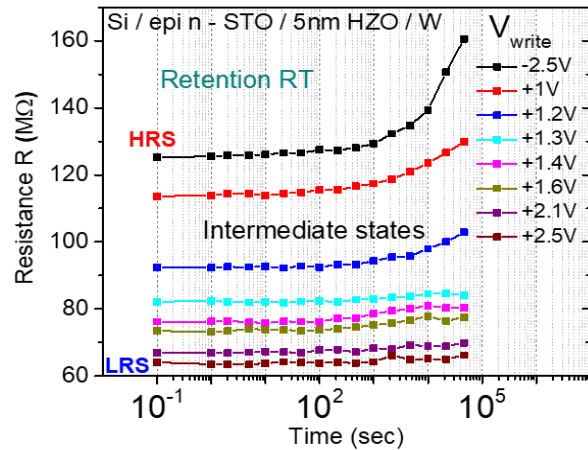


- Narrow memory window $\pm 1\text{V} \rightarrow$ compatible with ferroelectric switching ($V_c = 1\text{V}$)
- Many stable intermediate resistance states (16, 4bit)

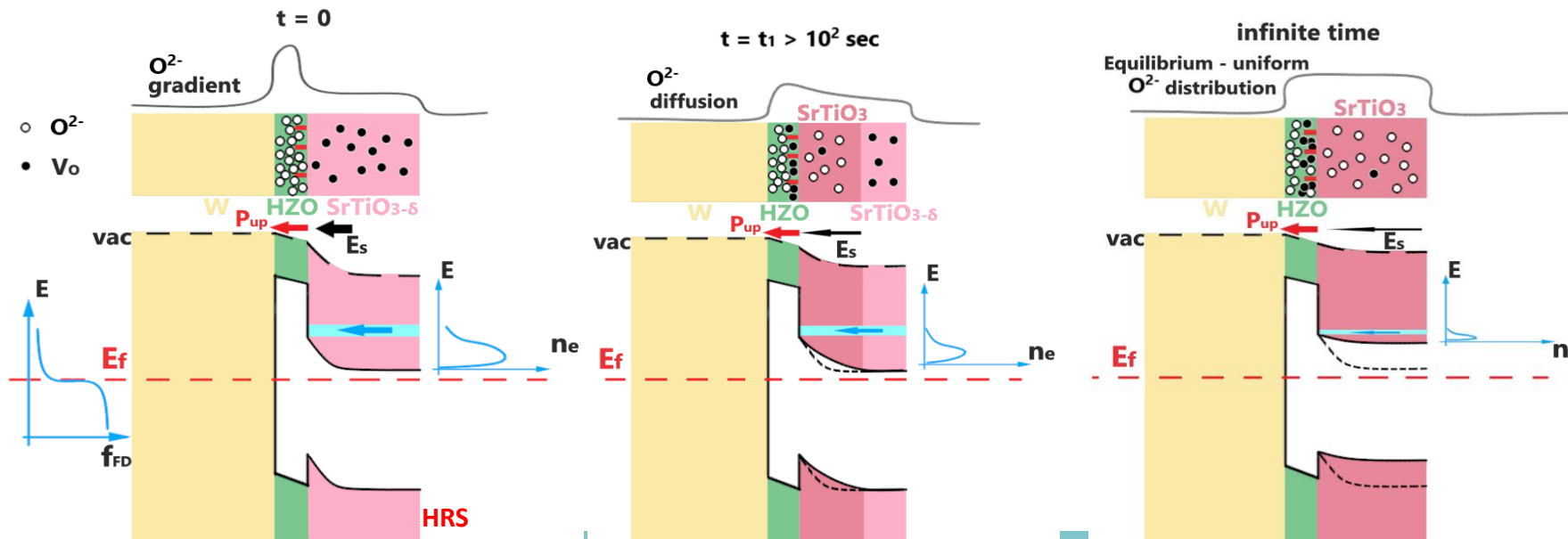


MAIN CHARACTERISTICS

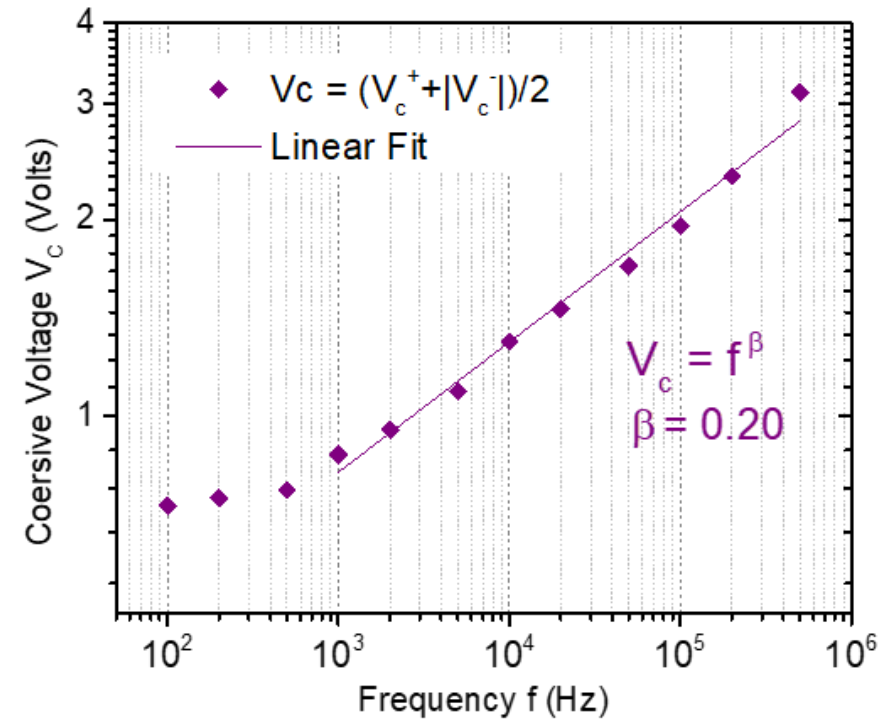
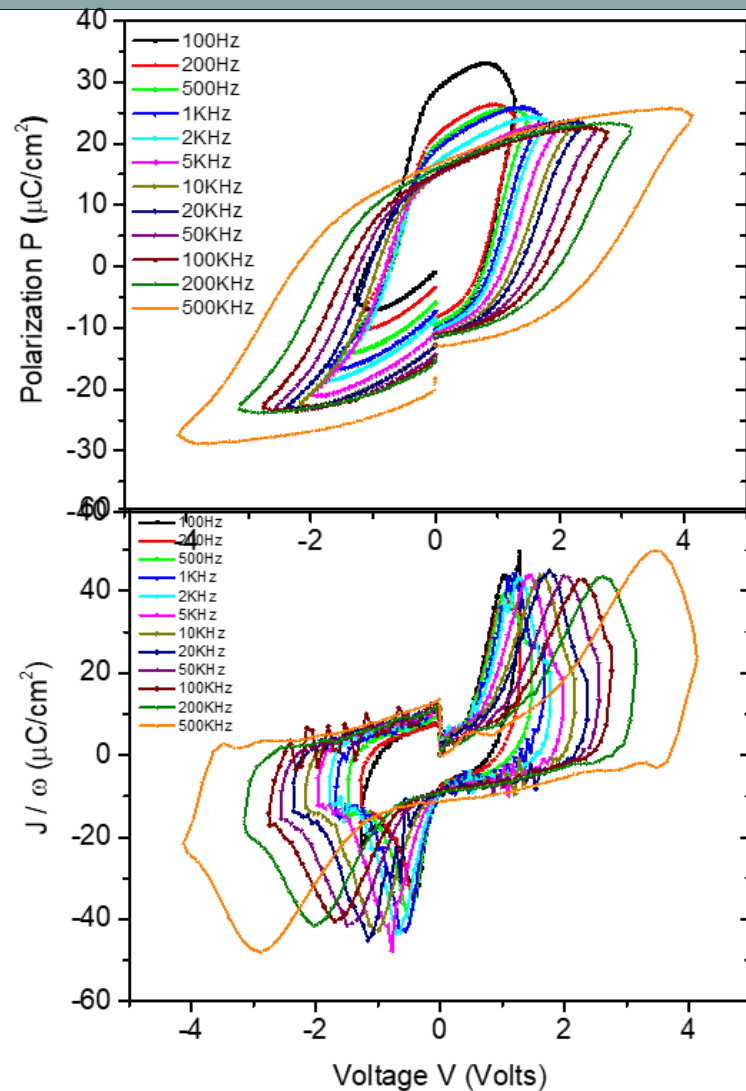
FIXIT



- HRS drifts to larger resistance
- Memory window increases at longer times !

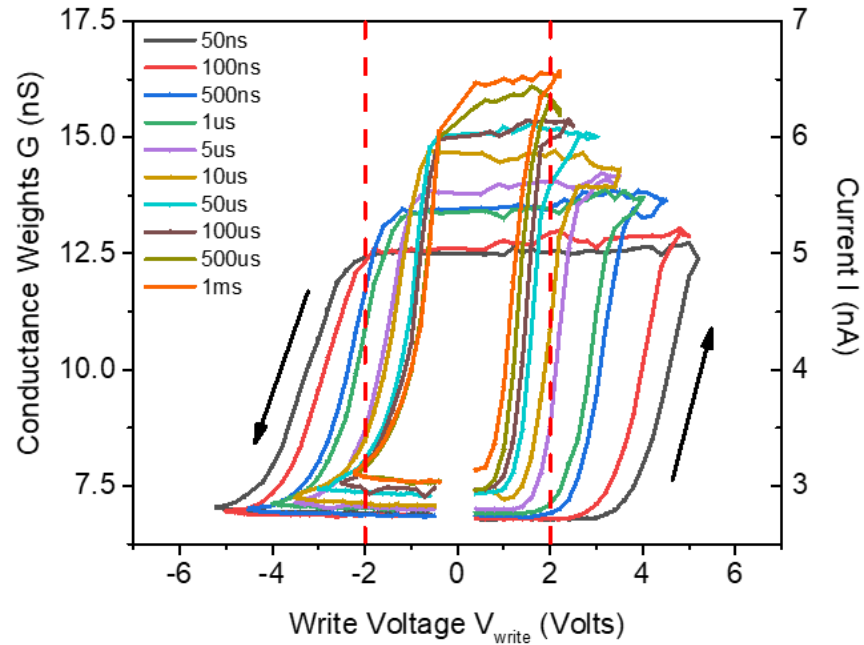


- O^{2-} acceptors diffuse inside STO and compensate the V_o donors
- STO becomes an intrinsic semiconductor increasing its resistance
- Ionic effects occur at shorter timescales too (< 1 ms)

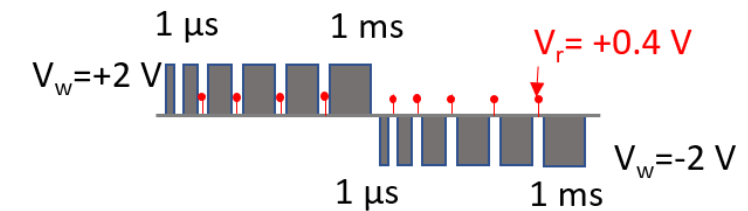
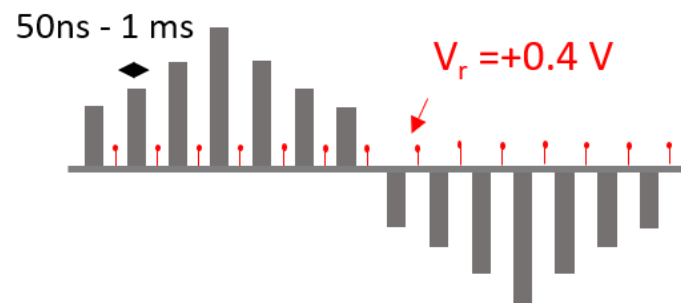
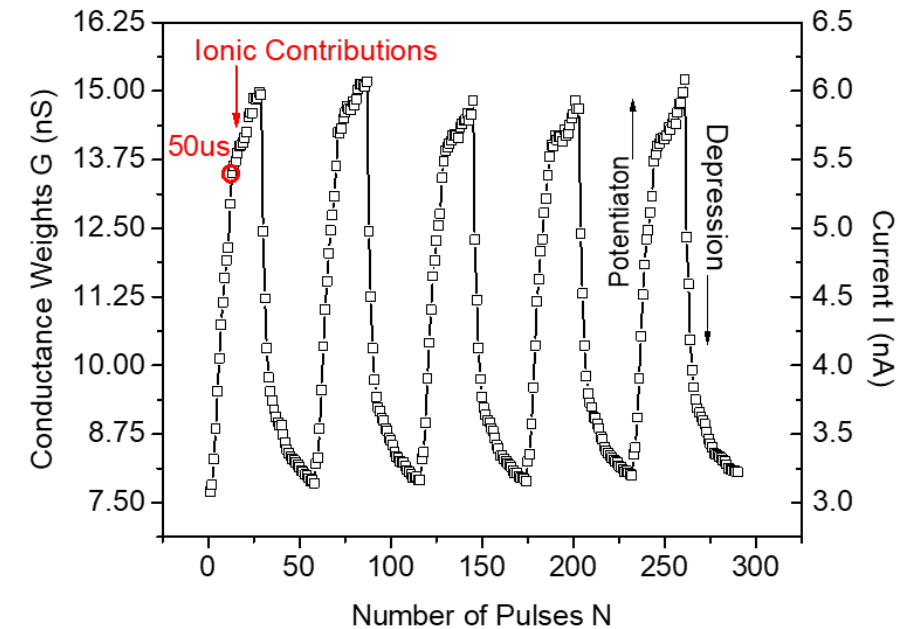


Typical behavior
for epitaxial ferroelectrics (e.g. perovskites)

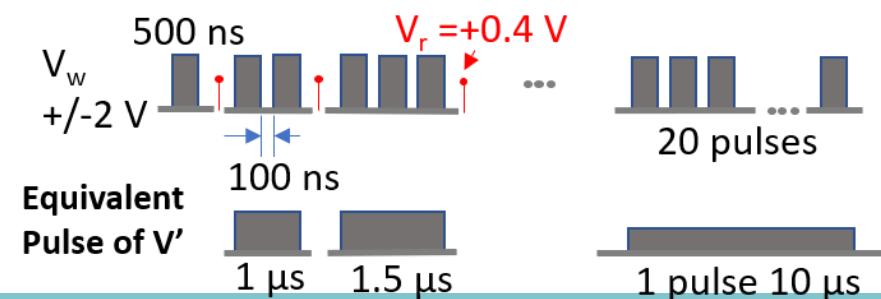
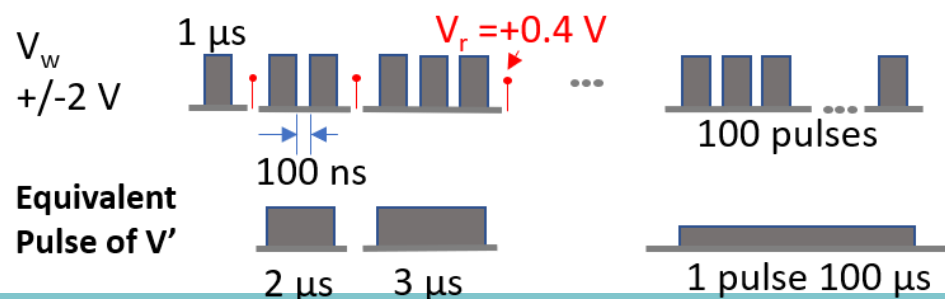
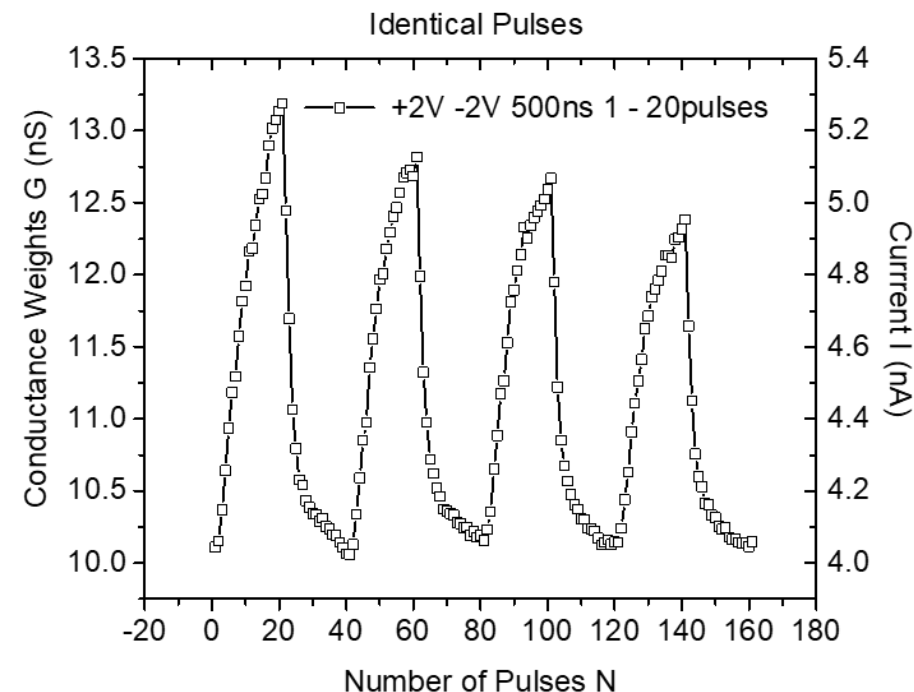
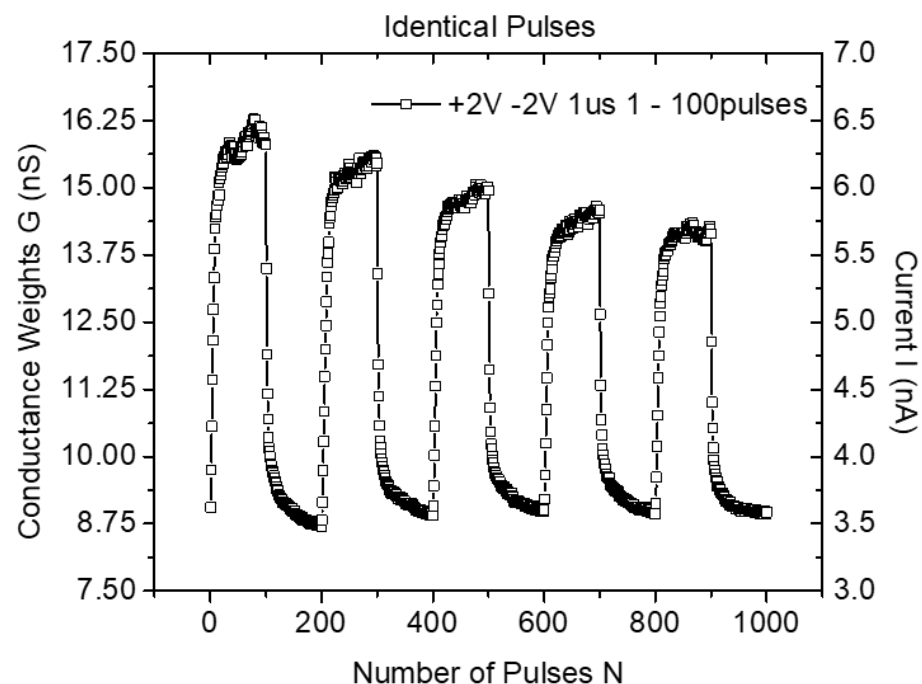
Time-voltage trade-off

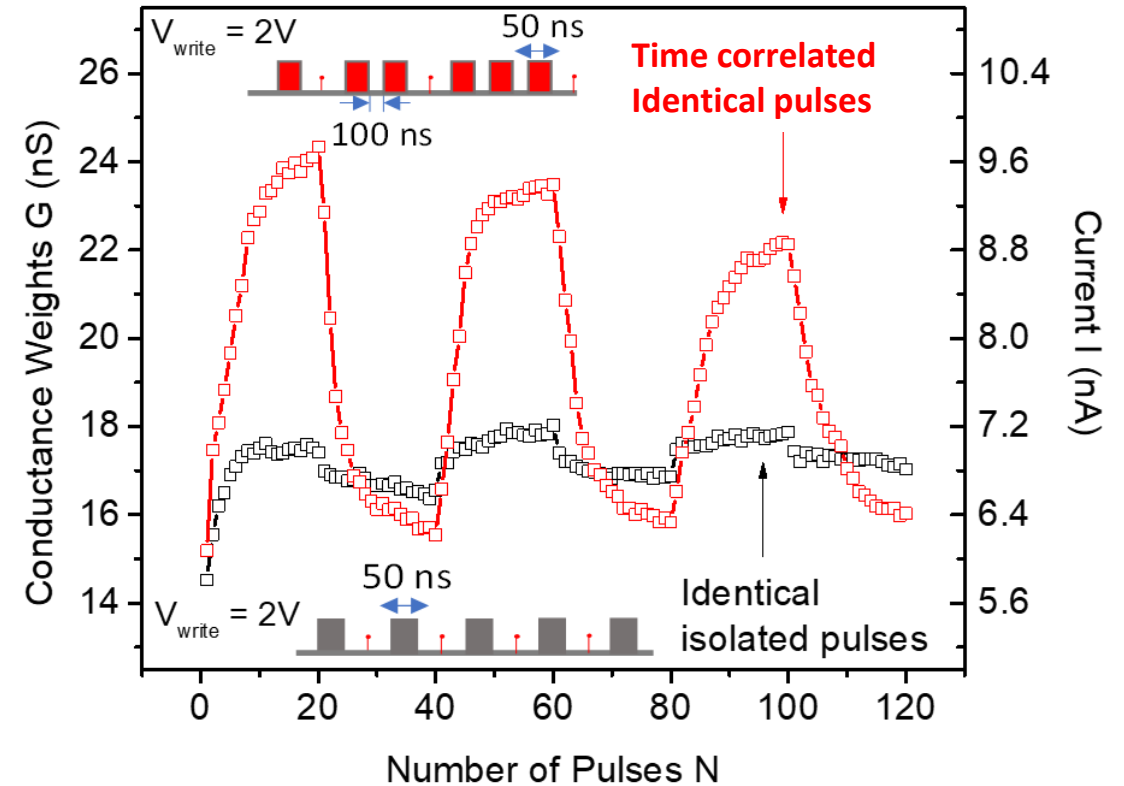
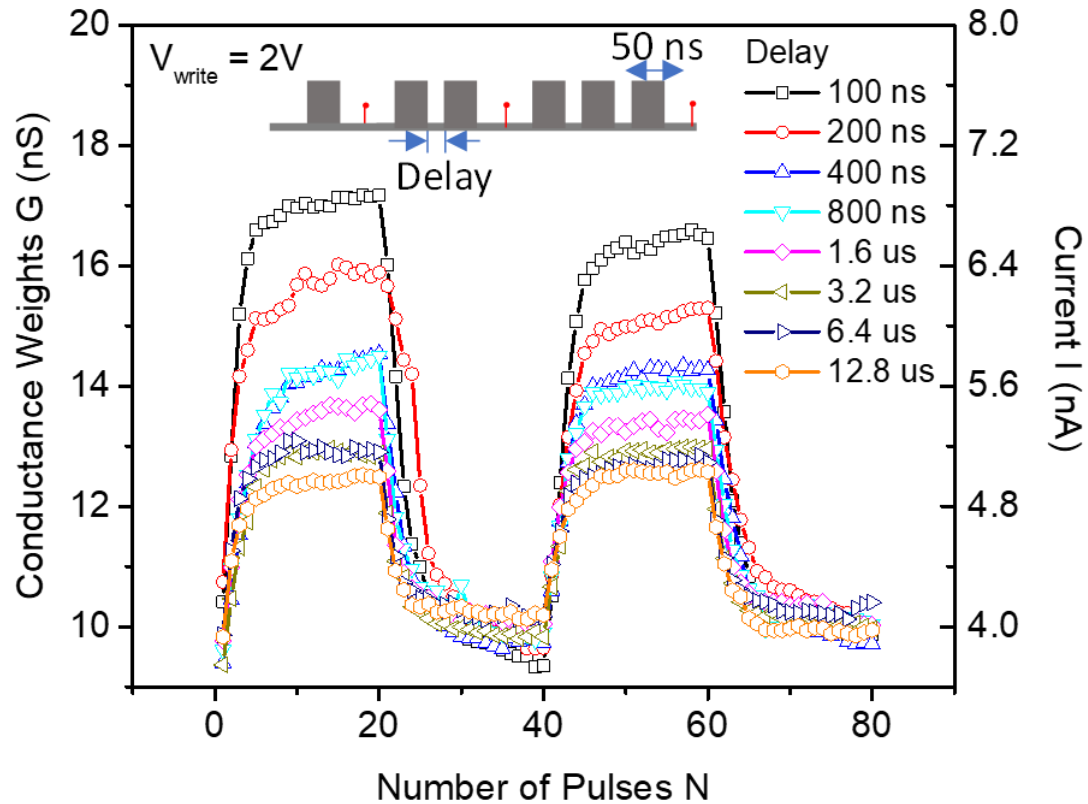


Variable width pulses

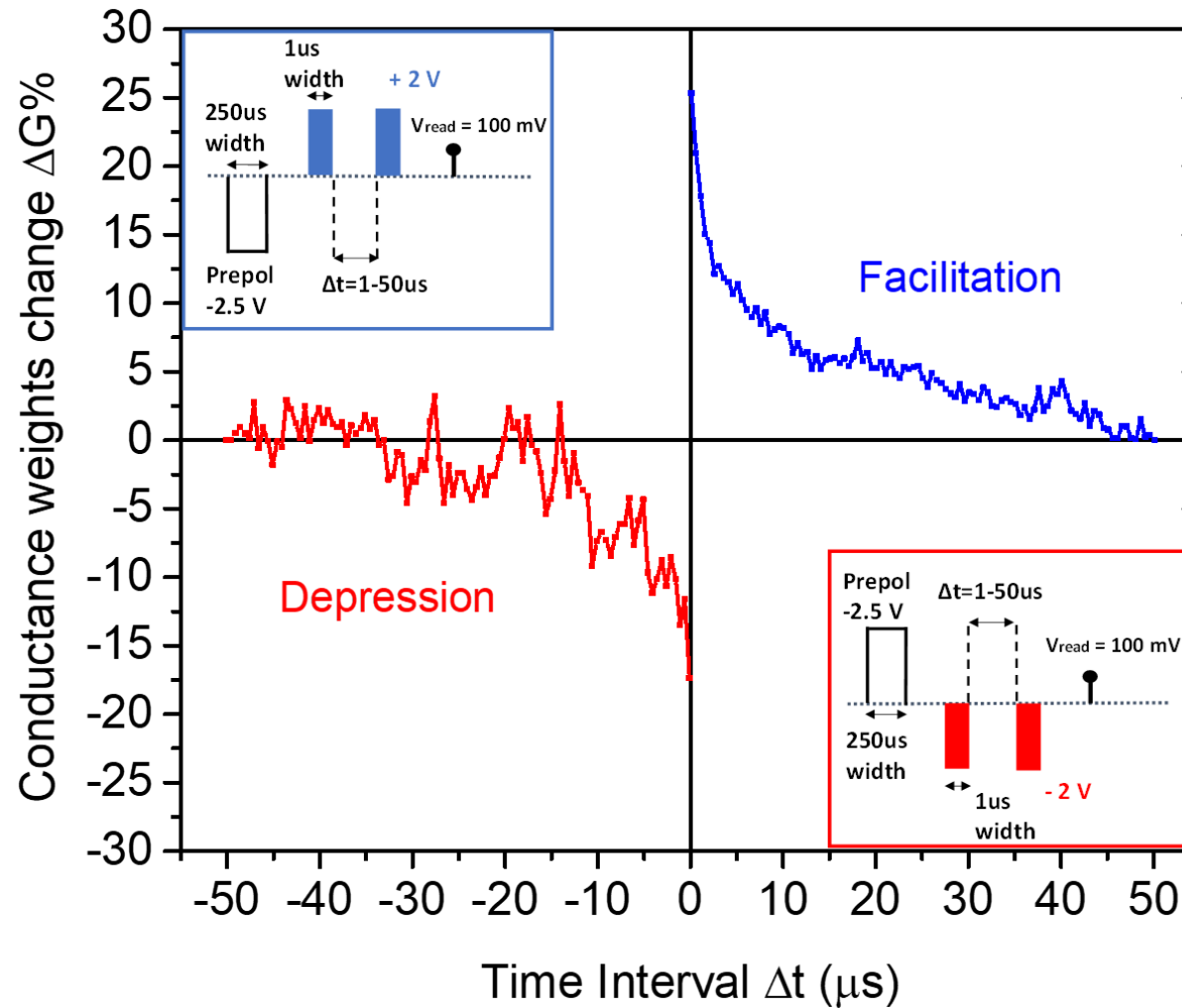


Also: M. Halter et al., *Commun. Mater* **4**, 14 (2023)





Synapse potentiation and depression is only possible with time correlated identical pulses (short delay)



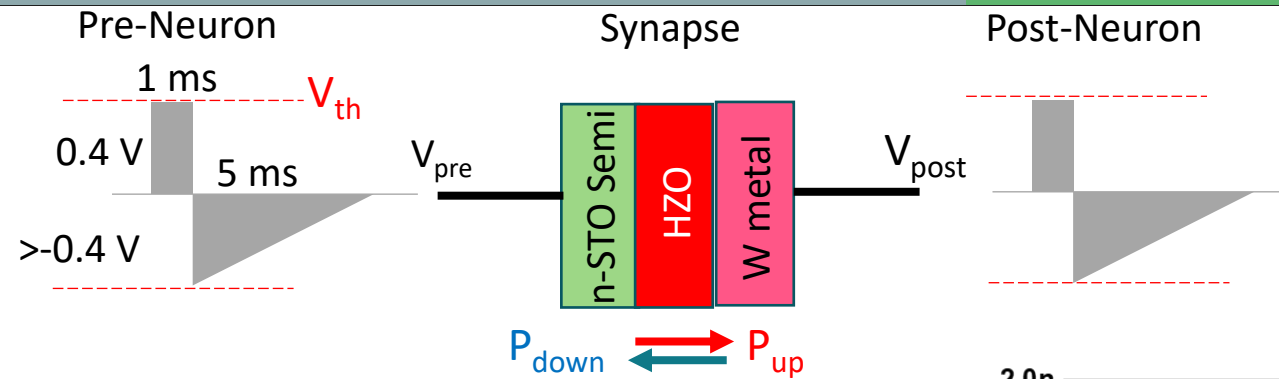
Short term plasticity

Decode temporary
audio/visual info
in biological systems

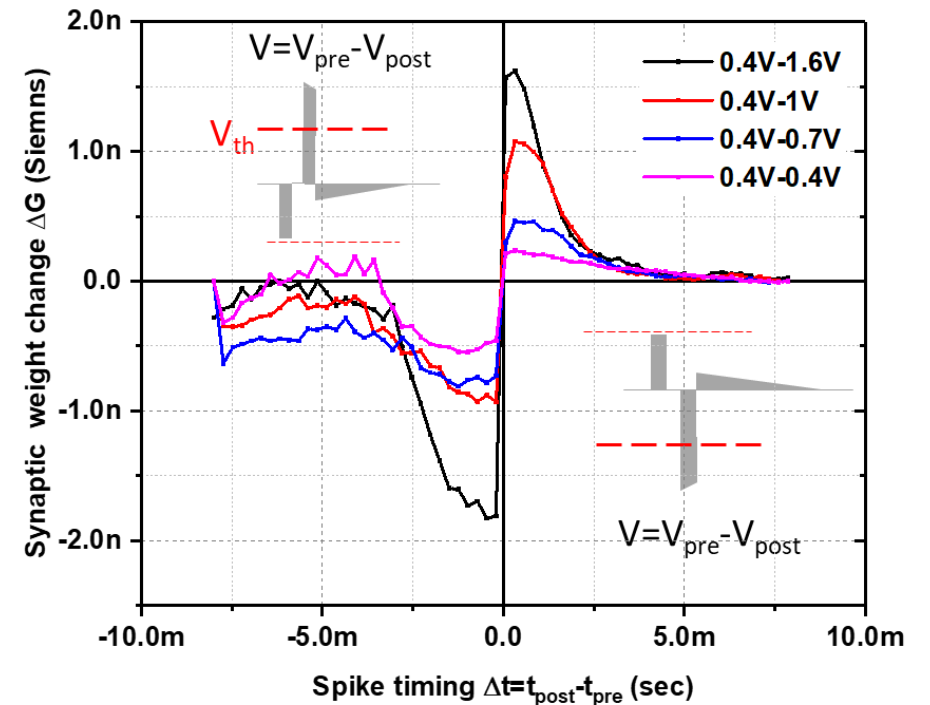
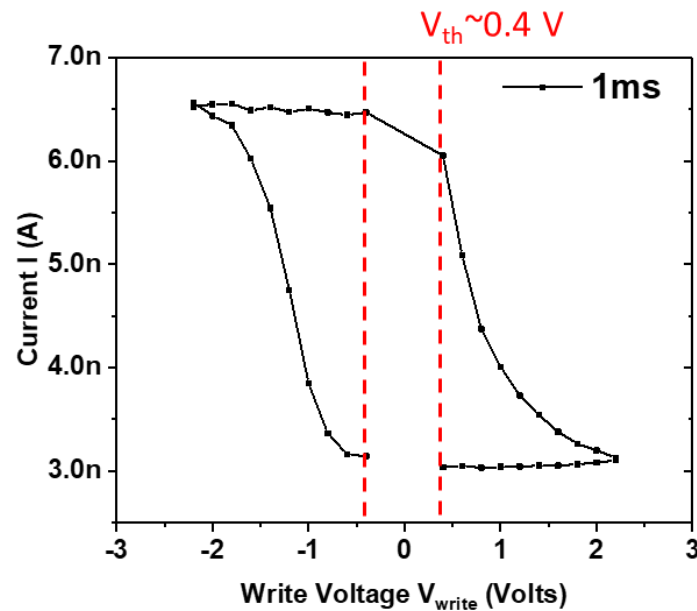
SPIKE TIMING DEPENDENT PLASTICITY (STDP)

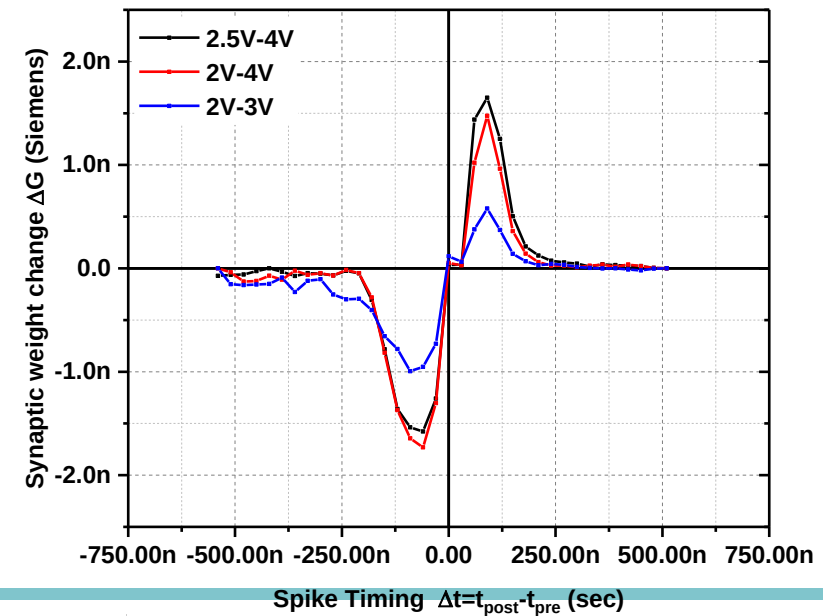
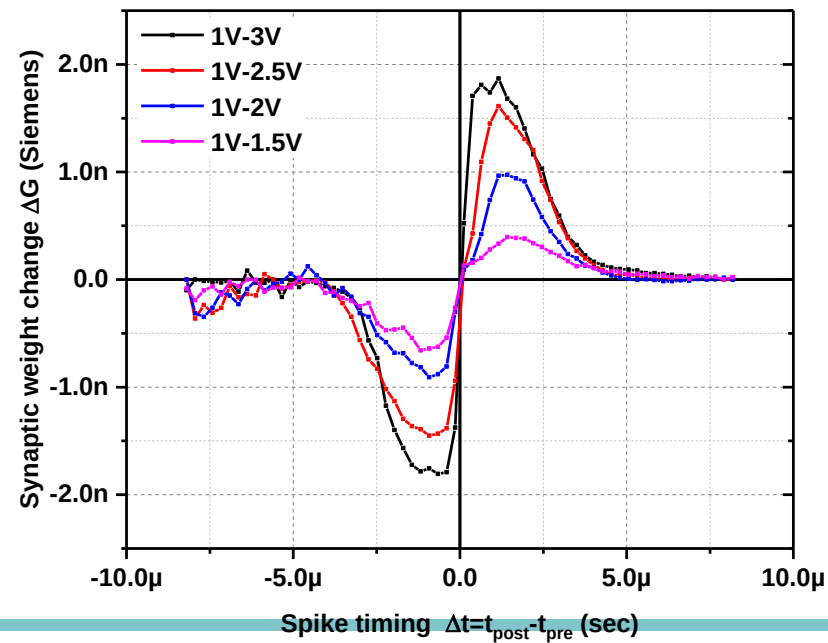
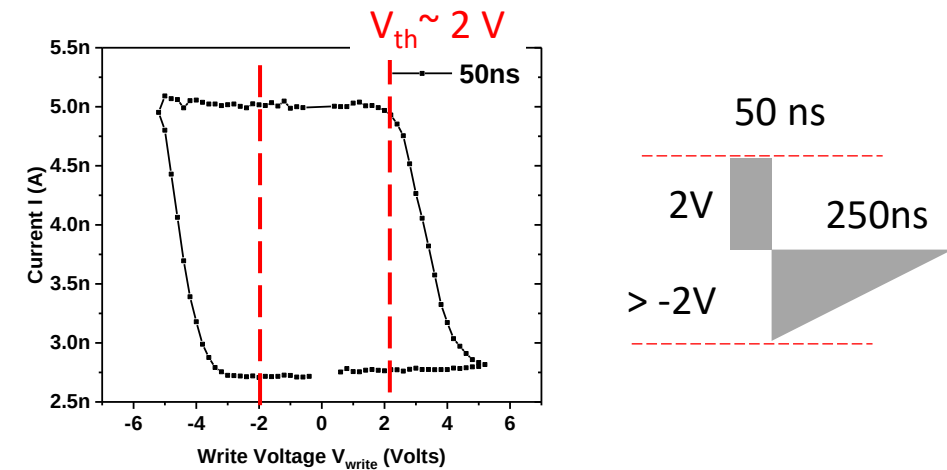
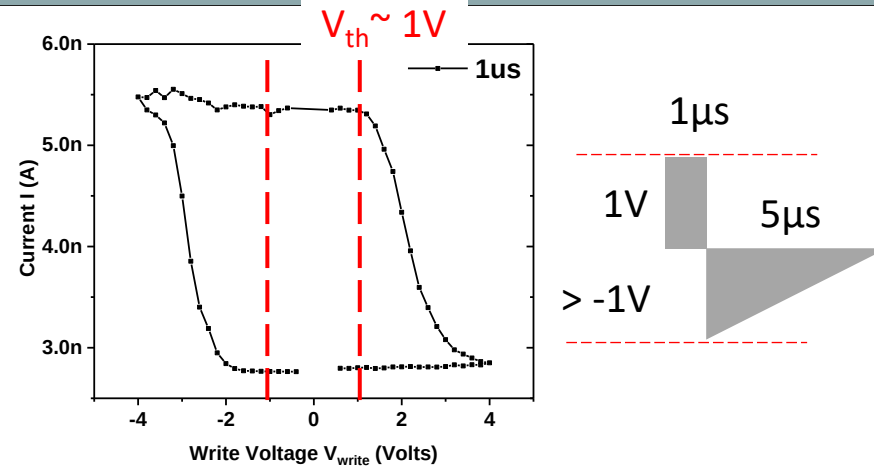
FIXIT

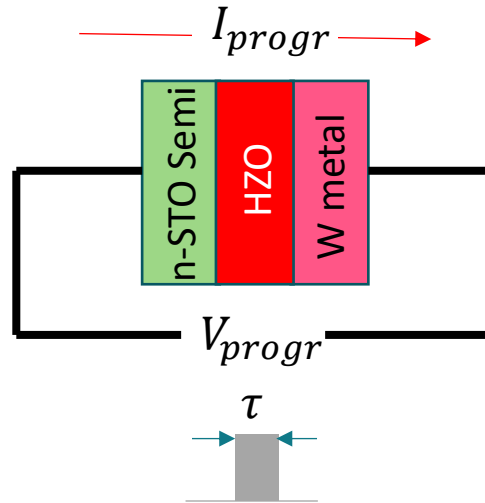
Hebbian learning in biological systems



Spiking Neural Networks







Current driven (RRAM, PCRAM, bio)
Energy spent as Joule heating

$$E = V_{progr} I_{progr} \tau$$

Voltage driven (FE)
Energy to charge a capacitor

$$E = QV = 2PAV$$

$$P = 20 \mu\text{C}/\text{cm}^2$$

$$V = 2\text{--}4 \text{ V}$$

$$A = 100 \times 100 \text{ nm}$$

	V_{prog}	I_{progr}	Pulse width τ	Energy E (Joule heat)	Energy (charging)	Area
Biological	10 mV	1 nA	1 ms	10 fJ		
RRAM	1V	10 μA	100 ns	1 pJ		
PCMRAM				10 pJ		
FTJ (our work)	2V	0.1 pA	1 ms	0.1 fJ	8 fJ	(100x100 nm)

- **Epitaxial HZO/STO/Si**
Ferroelectric field effect junctions-non volatile modulation of the STO semiconductor
- **Two effects:** electronic field effect + ionic redox → contribute additively enhancing performance
- **More than 16 stable intermediate states** can be accessed
- **Time to voltage trade off :**
Essential for potentiation and depression by variable width and identical pulses
- **Bio-inspired synaptic response:**
 - Pair pulse facilitation (PPF)
 - Spiking time dependent plasticity (STDP) operating at a large time range from ms to 100 ns
- **Extremely low energy per programming event:** ~ 10 fJ, comparable to biological synapses



NCSR: N. Siannas, C. Zacharaki, P. Tsipas and [A. Dimoulas](#)
Growth, processing, physical and electrical characterization



HZB: D.-J Kim W. Hamouda and C. Dubourdieu
Growth of epi n-STO/Si wafers



NIMP: C. Istrate and L. Pintilie
HR TEM



IKZ: M. Schmidbauer
X-ray Diffraction





BEOL technology platform based on ferroelectric synaptic devices for advanced neuromorphic processors

Work continues in HORIZON CL4 and JU-CHIPS projects



Scaled Ferroelectric X-bars for AI-driven sensors and actuators
Synaptic behavior in small area memristors



Crystalline Oxides for Next Generation Computing and Emerging Photonic Technologies
Epitaxial HZO, ionic effects



Vision Transformers with Ferroelectric Oxides
Integration



Artificial synapses based on ferroelectric tunnel junctions for neuromorphic and analogue computing

Chips JU KOR-EU

Romanian Recovery and Resilience Plan "ARSYF"

THANK YOU!

QUESTIONS?

